# Package 'LassoBacktracking' 

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## Type Package

Title Modelling Interactions in High-Dimensional Data with
Backtracking

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Author Rajen Shah [aut, cre]
Maintainer Rajen Shah [r.shah@statslab.cam.ac.uk](mailto:r.shah@statslab.cam.ac.uk)
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## Description

Perform k-fold cross-validation potentially multiple times on permuted version of the data.

## Usage

cvLassoBT(
x ,
$y$,
lambda = NULL,
nlambda $=100 \mathrm{~L}$,
lambda.min.ratio $=$ ifelse (nobs < nvars, 0.01, 1e-04),
nfolds $=5 \mathrm{~L}$,
nperms $=1 \mathrm{~L}$,
mc.cores $=1 \mathrm{~L}$,
)

## Arguments

\(\left.$$
\begin{array}{ll}\mathrm{x} & \text { input matrix of dimension nobs by nvars; each row is an observation vector. } \\
\mathrm{y} \\
\text { lambda } & \begin{array}{l}\text { response variable; shoud be a numeric vector. }\end{array}
$$ <br>
user supplied lambda sequence of decreasing penalty parameters. Typical usage <br>
is to allow the function to compute its own lambda sequence. Inappropriate <br>

sequences may cause convergence problems.\end{array}\right]\)| the number of lambda values. Must be at least 3. |
| :--- |

## Value

A list with components as below.
lambda the sequence of lambda values used
cvm a matrix of error estimates (with squared error loss). The rows correspond to different lambda values whilst the columns correspond to different iterations
BT_fit a "BT" object from a fit to the full data.
cv_opt a two component vector giving the cross-validation optimal lambda index and iteration
cv_opt_err the minimal cross-validation error.

## Examples

```
x <- matrix(rnorm(100*250), 100, 250)
y <- x[, 1] + x[, 2] - x[, 1]*x[, 2] + x[, 3] + rnorm(100)
out <- cvLassoBT(x, y, iter_max=10, nperms=2)
```

LassoBT Fit linear models with interactions using the Lasso.

## Description

Computes a number of Lasso solution paths with increasing numbers of interactions present in the design matrices corresponding to each path. Previous paths are used to speed up computation of subsequent paths so the process is very fast.

## Usage

```
    LassoBT(
        x,
        y,
        nlambda = 100L,
        iter_max = 1L,
        lambda.min.ratio = ifelse(nobs < nvars, 0.01, 1e-04),
        lambda = NULL,
        thresh = 1e-07,
        verbose = FALSE,
        inter_orig
    )
```


## Arguments

$x \quad$ input matrix of dimension nobs by nvars; each row is an observation vector.
y response variable; shoud be a numeric vector.
nlambda the number of lambda values. Must be at least 3 .
iter_max the number of iterations of the Backtracking algorithm to run. iter_max=1 corresponds to a single lasso or elasticnet fit. Values greater than 1 will fit interactions.
lambda.min.ratio
smallest value in lambda as a fraction of the largest value at which all main effects coefficients are 0 .

| lambda | user supplied lambda sequence of decreasing penalty parameters. Typical usage <br> is to allow the function to compute its own lambda sequence. Inappropriate <br> sequences may cause convergence problems. |
| :--- | :--- |
| thresh | convergence threshold for coordinate descent. Each inner coordinate descent <br> loop continues until either the maximum change in the objective after any coef- <br> ficient update is less than thresh or 1E5 iterations have been performed. <br> if TRUE will print iteration numbers. |
| verbose | an optional 2-row matrix with each column giving interactions that are to be |
| inter_orig | added to the design matrix before the algorithm begins. |

## Details

The Lasso optimisations are performed using coordinate descent similarly to the glmnet package. An intercept term is always included. Variables are centred and scaled to have equal empirical variance. Interactions are constructed from these centred and scaled variables, and the interactions themselves are also centred and scaled. Note the coefficients are returned on the original scale of the variables. Coefficients returned for interactions are for simple pointwise products of the original variables with no scaling.

## Value

An object with S3 class "BT".
call the call that produced the object
a0 list of intercept vectors
beta list of matrices of coefficients stored in sparse column format (CsparseMatrix)
fitted list of fitted values
lambda the sequence of lambda values used
nobs the number of observations
nvars the number of variables
var_indices the indices of the non-constant columns of the design matrix
interactions a 2-row matrix with columns giving the interactions that were added to the design matrix
path_lookup a matrix with columns corresponding to iterations and rows to lambda values. Entry $i j$ gives the component of the a 0 and beta lists that gives the coefficients for the $i$ th lambda value and $j$ th iteration
l_start a vector with component entries giving the minimimum lambda index in the corresponding copmonents of beta and a0

## References

Shah, R. D. (2016) Shah, R. D. (2016) Modelling interactions in high-dimensional data with Backtracking. JMLR, 17, l-3l https://www.jmlr.org/papers/volume17/13-515/13-515.pdf

## See Also

predict. BT, coef.BT methods and the cvLassoBT function.

## Examples

$x$ <- matrix(rnorm(100*250), 100, 250)
$y<-x[, 1]+x[, 2]-x[, 1] * x[, 2]+x[, 3]+\operatorname{rnorm}(100)$
out <- LassoBT(x, y, iter_max=10)

```
predict.BT Make predictions from a "BT" object.
```


## Description

Similar to other predict methods, this function predicts fitted values and computes coefficients from a fitted "BT" object.

## Usage

```
## S3 method for class 'BT'
predict(
    object,
    newx,
    s = NULL,
    iter = NULL,
    type = c("response", "coefficients"),
    ...
    )
    ## S3 method for class 'BT'
    coef(object, s = NULL, iter = NULL, ...)
```


## Arguments

| object | fitted "BT" object. |
| :--- | :--- |
| newx | matrix of new values of design matrix at which predictions are to be made. <br> Ignored when type=="coefficients". <br> value of the penalty parameter at which predictions are required. If the value is <br> not one of the lambda values present in object the output will be etermined by <br> linear interpolation. Default is the entire sequence of lambda values present in <br> object. <br> iteration at which predictions are required. Default is the entire sequence of <br> iterations in object. <br> of prediction required. Type "response" gives estimates of the response whilst <br> type "coefficients" gives coefficient estimates. |
| iter | not used. Other arguments to predict. |
| type |  |

## Value

Either a vector of predictions or, if either s or iter are NULL, a three-dimensional array with last two dimensions indexing different lambda values and iterations.

## Examples

```
x <- matrix(rnorm(100*250), 100, 250)
y <- x[, 1] + x[, 2] - x[, 1]*x[, 2] + x[, 3] + rnorm(100)
out <- LassoBT(x, y, iter_max=10)
predict(out, newx=x[1:2, ])
```


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