# Package 'GDAtools' 

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## Type Package

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Description Many tools for Geometric Data Analysis (Le Roux \& Rouanet (2005) [doi:10.1007/1-4020-2236-0](doi:10.1007/1-4020-2236-0)), such as MCA variants (Specific Multiple Correspondence Analysis, Class Specific Analysis), many graphical and statistical aids to interpretation (structuring factors, concentration ellipses, inductive tests, bootstrap validation, etc.) and multiple-table analysis (Multiple Factor Analysis, between- and inter-class analysis, Principal Component Analysis and Correspondence Analysis with Instrumental Variables, etc.).
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ahc.plots Plots for Ascending Hierarchical Clustering

## Description

Draws various plots for Ascending Hierarchical Clustering results.

## Usage

ahc.plots(ahc, distance $=$ NULL, max.cl $=20$, type = "dist")

## Arguments

| ahc | object of class hclust or agnes |
| :--- | :--- |
| distance | A dissimilarity matrix or a dist object. Only used if type is "inert" or "loss". |
| Default is NULL. |  |

## Details

The three kinds of plots proposed with this function are aimed at guiding in the choice of the number of clusters.

## Author(s)

Nicolas Robette

## See Also

```
dist.chi2
```


## Examples

```
data(Taste)
# clustering of a subsample of the data
disjonctif <- dichotom(Taste[1:200, 1:11])
distance <- dist(disjonctif)
cah <- stats::hclust(distance, method = "ward.D2")
# distance between aggregated clusters
ahc.plots(cah, max.cl = 15, type = "dist")
# percentage of explained inertia
ahc.plots(cah, distance = distance, max.cl = 15, type = "inert")
# relative loss of explained inertia
ahc.plots(cah, distance = distance, max.cl = 15, type = "loss")
```

angles.csa

Cosine similarities and angles between CSA and MCA

## Description

Computes the cosines similarities and angles between the components of a CSA and those of a MCA.

## Usage

angles.csa(rescsa, resmca)

## Arguments

| rescsa | object of class csMCA |
| :--- | :--- |
| resmca | object of class MCA or speMCA |

Value
A list of matrices:

| cosines | Cosine similarities |
| :--- | :--- |
| angles | Angles |

## Note

This function is adapted from csa.measures in sco. ca package.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

```
MCA, speMCA, csMCA
```


## Examples

```
## Performs a specific MCA and a CSA on the Music example data set
## and computes cosine similarities and angles
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
resmca <- speMCA(Music[,1:5], excl = junk)
female <- Music$Gender=="Women"
rescsa <- csMCA(Music[,1:5], subcloud = female, excl = junk)
angles.csa(rescsa, resmca)
```

barplot_contrib Bar plot of contributions

## Description

From MCA results, plots contributions to the axes.

## Usage

```
barplot_contrib(resmca, dim = 1, which = "var",
    sort = FALSE, col = "tomato4", repel = FALSE)
```


## Arguments

resmca object of class MCA, speMCA, csMCA, PCA or CA
dim the dimension to use. Default is 1.
which If resmca is of class MCA, speMCA, csMCA or PCA, should be "var" to plot contributions of variables or "ind" to plot contributions of individuals. If resmca is of class CA, should be "row" to plot contributions of rows or "col" to plot contributions of columns. Default is "var".
sort logical. If TRUE, bars are sorted by decreasing VIPs. Default is FALSE.
col color of the bars
repel logical. If TRUE, the names of the variables are repelled with geom_text_repel. Default is FALSE

## Details

The contributions are multiplied by the sign of the coordinates, so that the plot shows on which side of the axis they contribute, which makes the interpretation easier.

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

speMCA, tabcontrib

## Examples

```
# specific MCA on the Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# contributions of categories
barplot_contrib(mca)
```

```
bcMCA Between-class MCA
```


## Description

Between-class MCA, also called Barycentric Discriminant Analysis

## Usage

bcMCA(data, class, excl = NULL, row.w = NULL, ncp = 5)

## Arguments

data data frame with only categorical variables, i.e. factors
class factor specifying the class
excl numeric vector indicating the indexes of the "junk" categories (default is NULL). See getindexcat or use ijunk interactive function to identify these indexes. It may also be a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male").
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp $\quad$ number of dimensions kept in the results (by default 5)

## Details

Between-class MCA is sometimes also called Barycentric Discriminant Analysis or Discriminant Correspondence Analysis. It consists in three steps : 1. Transformation of data into an indicator matrix (i.e. disjunctive table) 2. Computation of the barycenter of the transformed data for each category of class 3. Correspondence Analysis of the set of barycenters Between-class MCA can also be viewed as a special case of MCA with instrumental variables, with only one categorical instrumental variable.

## Value

An object of class CA from FactoMineR package, with the indicator matrix of data as supplementary rows, and an additional item :
ratio the between-class inertia percentage

## Author(s)

Nicolas Robette

## References

Abdi H., 2007, "Discriminant Correspondence Analysis", In: Neil Salkind (Ed.), Encyclopedia of Measurement and Statistics, Thousand Oaks (CA): Sage.

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

DAQ, MCAiv

## Examples

```
library(FactoMineR)
data(tea)
res <- bcMCA(tea[,1:18], tea$SPC)
# categories of class
plot(res, invisible = c("col", "row.sup"))
# Variables in tea data
plot(res, invisible = c("row", "row.sup"))
# between-class inertia percentage
res$ratio
```

bcPCA Between-class Principal Component Analysis

## Description

Between-class Principal Component Analysis

## Usage

bcPCA(data, class, row.w = NULL, scale. unit = TRUE, ncp = 5)

## Arguments

| data | data frame with only numeric variables |
| :--- | :--- |
| class | factor specifying the class |
| row.w | numeric vector of row weights. If NULL (default), a vector of 1 for uniform row <br> weights is used. |
| scale.unit | logical. If TRUE (default) then data are scaled to unit variance. |
| ncp | number of dimensions kept in the results (by default 5) |

## Details

Between-class Principal Component Analysis consists in two steps: 1. Computation of the barycenter of data rows for each category of class 2. Principal Component Analysis of the set of barycenters

It is a quite similar to Linear Discriminant Analysis, but the metric is different.
It can be seen as a special case of PCA with instrumental variables, with only one categorical instrumental variable.

## Value

An object of class PCA from FactoMineR package, with the original data as supplementary individuals, and an additional item :
ratio the between-class inertia percentage

## Author(s)

Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

PCAiv, DA

## Examples

```
library(FactoMineR)
data(decathlon)
points <- cut(decathlon$Points, c(7300, 7800, 8000, 8120, 8900), c("Q1","Q2","Q3","Q4"))
res <- bcPCA(decathlon[,1:10], points)
# categories of class
plot(res, choix = "ind", invisible = "ind.sup")
# variables in decathlon data
plot(res, choix = "var")
# between-class inertia percentage
res$ratio
```

bootvalid_supvars Bootstrap validation (supplementary variables)

## Description

Bootstrap validation of MCA, through the computation of the coordinates of supplementary variables for bootstrap replications of the data.

## Usage

bootvalid_supvars(resmca, vars $=$ NULL, axes $=c(1,2), \mathrm{K}=30)$

## Arguments

resmea object of class speMCA.
vars a data frame of categorical supplementary variables. All these variables should be factors.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $c(1,2)$.
K integer. Number of bootstrap replications (default is 30 ).

## Details

The bootstrap technique is used here as an internal and non-parametric validation procedure of the results of a multiple correspondence analysis. For supplementary variables, only "partial bootstrap" is possible. The partial bootstrap does not compute new MCAs: it projects bootstrap replications of the initial data as supplementary elements of the MCA (see references for more details).

## Value

A data frame with the following elements :
varcat Names of the active categories
$\mathrm{K} \quad$ Indexes of the bootstrap replications
dim. $x \quad$ Bootstrap coordinates on the first selected axis
dim.y Bootstrap coordinates on the second selected axis

## Author(s)

Nicolas Robette

## References

Lebart L. (2006). "Validation Techniques in Multiple Correspondence Analysis". In M. Greenacre et J. Blasius (eds), Multiple Correspondence Analysis and related techniques, Chapman and Hall/CRC, p.179-196.

Lebart L. (2007). "Which bootstrap for principal axes methods?". In P. Brito et al. (eds), Selected Contributions in Data Analysis and Classification, Springer, p.581-588.

## See Also

ggbootvalid_supvars, bootvalid_variables

## Examples

```
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
    "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
    "Musical.NA")
resmca <- speMCA(Taste[,1:11], excl = junk)
supvars <- Taste[,c("Gender", "Age", "Educ")]
bv <- bootvalid_supvars(resmca, supvars, K = 5)
str(bv)
```

bootvalid_variables Bootstrap validation (active variables)

## Description

Bootstrap validation of MCA, through the computation of the coordinates of active variables for bootstrap replications of the data.

## Usage

bootvalid_variables(resmca, axes = c(1,2), type = "partial", K = 30)

## Arguments

resmca object of class speMCA.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
type character string. Can be "partial", "total1", "total2" or "total3" (see details). Default is "partial".
K integer. Number of bootstrap replications (default is 30).

## Details

The bootstrap technique is used here as an internal and non-parametric validation procedure of the results of a multiple correspondence analysis. Following the work of Ludovic Lebart, several methods are proposed. The "total bootstrap" uses new MCAs computed from bootstrap replications of the initial data. In the type 1 total bootstrap (type = "total1"), the sign of the coordinates is corrected if necessary (the direction of the axes of an ACM being arbitrary). In type 2 (type $=$ "total2"), the order of the axes and the sign of the coordinates are corrected if necessary. In type 3 (type = "total3"), a procrustean rotation is used to find the best superposition between the initial axes and the replicated axes. The "partial bootstrap"" (type = "partial") does not compute new MCAs: it projects bootstrap replications of the initial data as supplementary elements of the MCA. It gives a more optimistic view of the stability of the results than the total bootstrap. It also runs faster. See references for more details, pros and cons of the various types, etc.

Value
A data frame with the following elements :
varcat Names of the active categories
K Indexes of the bootstrap replications
dim. $x \quad$ Bootstrap coordinates on the first selected axis
dim.y Bootstrap coordinates on the second selected axis

## Author(s)

Nicolas Robette

## References

Lebart L. (2006). "Validation Techniques in Multiple Correspondence Analysis". In M. Greenacre et J. Blasius (eds), Multiple Correspondence Analysis and related techniques, Chapman and Hall/CRC, p.179-196.

Lebart L. (2007). "Which bootstrap for principal axes methods?". In P. Brito et al. (eds), Selected Contributions in Data Analysis and Classification, Springer, p.581-588.

## See Also

ggbootvalid_variables, bootvalid_supvars

## Examples

```
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
        "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
        "Musical.NA")
resmca <- speMCA(Taste[,1:11], excl = junk)
bv <- bootvalid_variables(resmca, type = "partial", K = 5)
str(bv)
```

burt

Burt table

## Description

Computes a Burt table from a data frame composed of categorical variables.

## Usage

burt(data)

## Arguments

data data frame with n rows (individuals) and p columns (categorical variables)

## Details

A Burt table is a symmetric table that is used in correspondence analysis. It shows the frequencies for all combinations of categories of pairs of variables.

## Value

Returns a square matrix. Its dimension is equal to the total number of categories in the data frame.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

dichotom

## Examples

```
## Burt table of variables in columns 1 to 5
## in the Music example data set
data(Music)
burt(Music[,1:5])
```

    coiMCA Coinertia analysis between two groups of categorical variables
    
## Description

Coinertia analysis between two groups of categorical variables

## Usage

coiMCA(Xa, Xb,
excl.a = NULL, excl.b = NULL,
row.w = NULL, ncp = 5)

## Arguments

Xa
$\mathrm{Xb} \quad$ data frame with the second group of categorical variables
excl.a numeric vector indicating the indexes of the "junk" categories in Xa (default is NULL). See getindexcat or use ijunk interactive function to identify these indexes. It may also be a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male").
excl.b numeric vector indicating the indexes of the "junk" categories in Xb (default is NULL). See excl.a argument.
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp $\quad$ number of dimensions kept in the results (by default 5)

## Details

Coinertia analysis aims at capturing the structure common to two groups of variables. With groups of numerical variables, it is equivalent to Tucker's inter-battery analysis. With categorical data, it consists in the following steps : 1. Transformation of Xa and Xb into indicator matrices (i.e. disjunctive tables) Xad and Xbd 2. Computation of the covariance matrix $t(X a d) . X b d$ 3. CA of the matrix

## Value

An object of class CA from FactoMineR package, with an additional item :
RV the RV coefficient between the two groups of variabels

## Author(s)

Nicolas Robette

## References

Tucker, L.R.. (1958) An inter-battery method of factor analysis. Psychometrika, 23-2, 111-136.
Dolédec, S. and Chessel, D. (1994) Co-inertia analysis: an alternative method for studying speciesenvironment relationships. Freshwater Biology, 31, 277-294.

## See Also

coiPCA, rvcoef

## Examples

```
data(Music)
# music tastes
Xa <- Music[,1:5]
# gender and age
Xb <- Music[,6:7]
```

```
# coinertia analysis
res <- coiMCA(Xa, Xb)
plot(res)
# RV coefficient
res$RV
```

coiPCA Coinertia analysis between two groups of numerical variables

## Description

Coinertia analysis between two groups of numerical variables

## Usage

coiPCA(Xa, Xb, row.w = NULL, ncp = 5)

## Arguments

Xa data frame with the first group of numerical variables
$\mathrm{Xb} \quad$ data frame with the second group of numerical variables
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp number of dimensions kept in the results (by default 5)

## Details

Coinertia analysis aims at capturing the structure common to two groups of variables. With groups of numerical variables, it is equivalent to Tucker's inter-battery analysis. It consists in the following steps : 1. Variables in Xa and Xb are centered and scaled 2. Computation of the covariance matrix $\mathrm{t}(\mathrm{Xa}) \cdot \mathrm{Xb} 3$. PCA of the matrix

## Value

An object of class PCA from FactoMineR package, with an additional item :
RV the RV coefficient between the two groups of variabels

## Author(s)

Nicolas Robette

## References

Tucker, L.R. (1958) An inter-battery method of factor analysis. Psychometrika, 23-2, 111-136.
Dolédec, S. and Chessel, D. (1994) Co-inertia analysis: an alternative method for studying speciesenvironment relationships. Freshwater Biology, 31, 277-294.

## See Also

coiMCA, rvcoef

## Examples

```
library(FactoMineR)
data(decathlon)
# variables of results for each sport
Xa <- decathlon[,1:10]
# rank and points variables
Xb <- decathlon[,11:12]
# coinertia analysis
res <- coiPCA(Xa, Xb)
# plot of variables in Xa
plot(res, choix = "ind")
# plot of variables in Xb
plot(res, choix = "var")
# RV coefficient
res$RV
```

```
conc.ellipse
Concentration ellipses
```


## Description

Adds concentration ellipses or other kinds of inertia ellipses to the cloud of individuals of a MCA.

## Usage

```
conc.ellipse(resmca, var, sel = 1:nlevels(var), axes = c(1, 2),
    kappa = 2, col = rainbow(length(sel)), pcol = rainbow(length(sel)), pcex = 0.2,
    lty = 1, lwd = 1, tcex = 1, text.lab = TRUE)
```


## Arguments

\(\left.\begin{array}{ll}resmca \& object of class MCA, speMCA, csMCA, multiMCA or stMCA <br>

var \& supplementary variable to plot\end{array}\right]\)| numeric vector of indexes of the categories to plot (by default, ellipses are plot- |
| :--- |
| ted for every categories) |
| axes |
| kappa |
| length 2 vector specifying the components to plot (default is c(1,2)) |
| col |
| pcol | | numeric. The kappa value (i.e. "index") of the inertia ellipses. By default, kappa |
| :--- |
| $=2$, which means that concentration ellipses are plotted. |
| vector of colors for the ellipses of plotted categories (by default, rainbow palette |
| is used) |
| vector of colors for the points at the center of ellipses of plotted categories (by |
| default, rainbow palette is used) |


| pcex | numerical value giving the amount by which points at the center of ellipses <br> should be magnified (default is 0.2 ) |
| :--- | :--- |
| lty | line type for ellipses (default is 1 ) |
| lwd | line width for the ellipses (default is 1 ) |
| tcex | numerical value giving the amount by which labels at the center of ellipses <br> should be magnified (default is 0.2 ) |
| text.lab | whether the labels at the center of ellipses should be displayed (default is TRUE) |

## Details

If kappa=2, ellipses are called "concentration" ellipses and, for a normally shaped subcloud, contain 86.47 percents of the points of the subcloud. If kappa=1, ellipses are "indicator" ellipses and contain 39.35 percents of the points of the subcloud. If kappa=1.177, ellipses are "median" ellipses and contain 50 percents of the points of the subcloud. This function has to be used after the cloud of individuals has been drawn.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

plot.speMCA, plot.csMCA, plot.multiMCA, plot.stMCA

## Examples

```
## Performs specific MCA (excluding 'NA' categories) of 'Taste' example data set,
## plots the cloud of categories
## and adds concentration ellipses for gender variable
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
            "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
            "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
plot(mca, type = "i")
conc.ellipse(mca, Taste$Gender)
## Draws a blue concentration ellipse for men only
plot(mca, type = "i")
conc.ellipse(mca, Taste$Gender, sel = 1, col = "blue")
```


## Description

From MCA results, computes contributions of categories and variables to the axes and the overall cloud.

## Usage

contrib(resmca)

## Arguments

```
    resmca object of class MCA, speMCA or csMCA
```


## Details

The contribution of a point to an axis depends both on the distance from the point to the origin point along the axis and on the weight of the point. The contributions of points to axes are the main aid to interpretation (see Le Roux and Rouanet, 2004 and 2010).

## Value

A list of data frames:
ctr Data frame with the contributions of categories to axes
var.ctr Data frame with the contributions of variables to axes
ctr.cloud Data frame with the contributions of categories to the overall cloud
vctr.cloud Data frame with the contributions of variables to the overall cloud

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

```
speMCA, supvar, tabcontrib
```


## Examples

```
# specific MCA on the Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# contributions of variables
contrib(mca)
```

csMCA Class Specific Analysis

## Description

Performs a "class specific"" Multiple Correspondence Analysis, i.e. a variant of MCA consisting in analyzing a subcloud of individuals.

## Usage

csMCA(data, subcloud $=$ rep(TRUE, times $=$ nrow(data)), excl = NULL, ncp = 5, row.w $=\operatorname{rep}(1$, times $=\operatorname{nrow}($ data) $)$ )

## Arguments

| data | data frame with $n$ rows (individuals) and $p$ columns (categorical variables) |
| :--- | :--- |
| subcloud | a vector of logical values and length n. The subcloud of individuals analyzed <br> with class specific MCA is made of the individuals with value TRUE. |
| excl | nnumeric vector indicating the indexes of the "junk" categories (default is NULL). <br> See getindexcat or use i junk interactive function to identify these indexes. It <br> may also be a character vector of junk categories, specified in the form "namevari- <br> able.namecategory" (for instance "gender.male"). |
| ncp | number of dimensions kept in the results (default is 5) <br> row.w |
| an optional numeric vector of row weights (by default, a vector of 1 for uniform <br> row weights) |  |

## Details

This variant of MCA is used to study a subset of individuals with reference to the whole set of individuals, i.e. to determine the specific features of the subset. It consists in proceeding to the search of the principal axes of the subcloud associated with the subset of individuals (see references).

## Value

An object of class csMCA, i.e. a list including:
eig a list of vectors containing all the eigenvalues, the percentage of variance, the cumulative percentage of variance, the modified rates and the cumulative modified rates

| call | a list with informations about input data |
| :--- | :--- |
| ind | a list of matrices containing the results for the individuals (coordinates, contri- <br> butions) |
| var | a list of matrices containing all the results for the categories and variables (weights, <br> coordinates, squared cosines, categories contributions to axes and cloud, test val- <br> ues (v.test), squared correlation ratio (eta2), variable contributions to axes and <br> cloud |

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ijunk, speMCA

## Examples

```
# class specific MCA of the subcloud of women
# from the Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
female <- Music$Gender=="Women"
mca <- csMCA(Music[,1:5],
        subcloud = female,
        excl = junk)
plot(mca)
```


## Description

Descriptive discriminant analysis, aka "Analyse Factorielle Discriminante" for the French school of multivariate data analysis.

## Usage

DA(data, class, row.w = NULL, type = "FR")

## Arguments

data data frame with only numeric variables
class factor specifying the class
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
type If "FR" (default), the inverse of the total covariance matrix is used as metric. If "GB", it is the inverse of the within-class covariance matrix (Mahalanobis metric), which makes the results equivalent to linear discriminant analysis as implemented in lda function in MASS package.

## Details

The results are the same with type "FR" or "GB", only the eigenvalues vary. With type="FR", these eigenvalues vary between 0 and 1 and can be interpreted as "discriminant power".

## Value

An object of class PCA from FactoMineR package, with class as qualitative supplementary variable, and one additional item :
cor_ratio correlation ratios between class and the discriminant factors

## Note

The code is adapted from a script from Marie Chavent. See: https://marie-chavent.perso.math.cnrs.fr/teaching/

## Author(s)

Marie Chavent, Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)
Saporta G., 2006, Probabilités, analyses des données et statistique, Editions Technip.

## See Also

bcPCA, PCAiv

## Examples

```
library(FactoMineR)
data(decathlon)
points <- cut(decathlon$Points, c(7300, 7800, 8000, 8120, 8900), c("Q1","Q2","Q3","Q4"))
res <- DA(decathlon[,1:10], points)
# plot of observations colored by class
plot(res, choix = "ind", invisible = "quali", habillage = res$call$quali.sup$numero)
```

```
# plot of class categories
plot(res, choix = "ind", invisible = "ind", col.quali = "darkblue")
# plot of variables
plot(res, choix = "varcor", invisible = "none")
```


## Description

Descriptive discriminant analysis (aka "Analyse Factorielle Discriminante" for the French school of multivariate data analysis) with qualitative variables.

## Usage

DAQ(data, class, excl = NULL, row.w = NULL, type = "FR", select = TRUE)

## Arguments

data data frame with only categorical variables
class factor specifying the class
excl numeric vector indicating the indexes of the "junk" categories (default is NULL). See getindexcat or use ijunk interactive function to identify these indexes. It may also be a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male").
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
type character string. If "FR" (default), the inverse of the total covariance matrix is used as metric. If "GB", it is the inverse of the within-class covariance matrix (Mahalanobis metric), which makes the results equivalent to linear discriminant analysis as implemented in lda function in MASS package.
select logical. If TRUE (default), only a selection of components of the MCA are used for the discriminant analysis step. The selected components are those corresponding to eigenvalues higher of equal to $1 / \mathrm{Q}$, with Q the number of variables in data. If FALSE, all components are used.

## Details

This approach is also known as "disqual" and was developed by G. Saporta (see references). It consists in two steps : 1. Multiple Correspondence Analysis of the data 2. Discriminant analysis of the components from the MCA
The results are the same with type "FR" or "GB", only the eigenvalues vary. With type="FR", these eigenvalues vary between 0 and 1 and can be interpreted as "discriminant power".

## Value

An object of class PCA from FactoMineR package, with class as qualitative supplementary variable and the disjunctive table of data as quantitative supplementary variables, and two additional items :
cor_ratio correlation ratios between class and the discriminant factors
mca an object of class speMCA with the results of the MCA of the first step

## Note

If there are NAs in data, these NAs will be automatically considered as junk categories. If one desires more flexibility, data should be recoded to add explicit factor levels for NAs and then excl option may be used to select the junk categories.

## Author(s)

Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

Saporta G., 1977, "Une méthode et un programme d'analyse discriminante sur variables qualitatives", Premières Journées Internationales, Analyses des données et informatiques, INRIA, Rocquencourt.
Saporta G., 2006, Probabilités, analyses des données et statistique, Editions Technip.

## See Also

DA, bcMCA, MCAiv, speMCA

## Examples

```
library(FactoMineR)
data(tea)
res <- DAQ(tea[,1:18], tea$SPC)
# plot of observations colored by class
plot(res, choix = "ind", invisible = "quali",
    label = "quali", habillage = res$call$quali.sup$numero)
# plot of class categories
plot(res, choix = "ind", invisible = "ind", col.quali = "black")
# plot of the variables in data
plot(res, choix = "var", invisible = "var")
# plot of the components of the MCA
plot(res, choix = "varcor", invisible = "quanti.sup")
```


## Description

Dichotomizes the variables in a data frame exclusively composed of categorical variables, i.e. transforms the data into an indicator matrix (also known as disjunctive table)

## Usage

dichotom(data, out = "numeric")

## Arguments

data data frame of categorical variables
out character string defining the format for dichotomized variables in the output data frame. Format may be "numeric" (default) or "factor".

## Value

Returns a data frame with dichotomized variables. The number of columns is equal to the total number of categories in the input data.

## Author(s)

Nicolas Robette, Julien Barnier

## Examples

```
## Dichotomizes Music example data frame
data(Music)
dic <- dichotom(Music[,1:5])
str(dic)
## with output variables in factor format
dic <- dichotom(Music[,1:5], out='factor')
str(dic)
```


## Description

Dichotomizes the factor variables in a data frame composed of mixed format variables, i.e. transforms the factors into an indicator matrix (also known as disjunctive table) and keeps the numerical variables.

## Usage

dichotomixed(data, out = "numeric")

## Arguments

data data frame of categorical and numerical variables
out character string defining the format for dichotomized variables in the output data frame. Format may be "numeric" (default) or "factor".

## Value

Returns a data frame with numerical variables and dichotomized factor variables

## Author(s)

Nicolas Robette

## Examples

```
## Dichotomizes Music example data frame
data(Music)
## recodes Age as numerical, for the sake of the example
Music$Age <- as.numeric(Music$Age)
## dichotomization
dic <- dichotomixed(Music)
str(dic)
```

dimcontrib
Description of the contributions to axes

## Description

Identifies the categories and individuals that contribute the most to each dimension obtained by a Multiple Correspondence Analysis.

## Usage

dimcontrib(resmca, $\operatorname{dim}=c(1,2)$, best $=$ TRUE)

## Arguments

resmca object of class MCA, speMCA, or csMCA
dim numerical vector of the dimensions to describe (default is $\mathrm{c}(1,2)$ )
best logical. If FALSE, displays all the categories. If TRUE (default), displays only categories and individuals with contributions higher than average

## Details

Contributions are sorted and assigned a positive or negative sign according to the corresponding categories or individuals coordinates, so as to facilitate interpretation.

## Value

Returns a list with the following items :
var a list of categories contributions to axes
ind a list of individuals contributions to axes

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

tabcontrib, dimdescr, dimeta2, dimtypicality

## Examples

```
# specific MCA on Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# contributions to axes 1 and 2
dimcontrib(mca)
```


## Description

Identifies the variables and the categories that are the most characteristic according to each dimension obtained by a MCA. It is inspired by dimdesc function in FactoMineR package (see Husson et al, 2010), but allows to analyze variants of MCA, such as specific MCA or class specific MCA.

## Usage

dimdescr (resmca, vars $=$ NULL, $\operatorname{dim}=c(1,2)$,
limit = NULL, correlation = "pearson",
na.rm.cat $=$ FALSE, na.value.cat $=$ "NA", na.rm.cont $=$ FALSE, nperm = NULL, distrib = "asympt", shortlabs = TRUE)

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multimCA
vars data frame of variables to describes the MCA dimensions with. If NULL (default), the active variables of the MCA will be used.
dim the dimensions which are described. Default is $\mathrm{c}(1,2)$
limit for the relationship between a dimension and a categorical variable, only associations (measured with point-biserial correlations) higher or equal to limit will be displayed. If NULL (default), they are all displayed.
correlation character string. The type of correlation measure to be used between two numerical variables : "pearson" (default), "spearman" or "kendall".
na.rm.cat logical, indicating whether NA values in the categorical variables should be silently removed before the computation proceeds. If FALSE (default), an additional level is added to the categorical variables (see na.value.cat argument).
na.value.cat character string. Name of the level for NA category. Default is "NA". Only used if na.rm. cat $=$ FALSE.
na.rm. cont logical indicating whether NA values in the numerical variables should be silently removed before the computation proceeds. Default is FALSE.
nperm numeric. Number of permutations for the permutation tests of independence. If NULL (default), no permutation test is performed.
distrib the null distribution of permutation test of independence can be approximated by its asymptotic distribution ("asympt", default) or via Monte Carlo resampling ("approx").
shortlabs logical. If TRUE (default), the data frame will have short column names, so that all columns can be displayed side by side on a laptop screen.

## Details

See condesc.

## Value

Returns a list of ncp lists including:
variables associations between dimensions of the MCA and the variables in vars
categories a data frame with categorical variables from vars and associations measured by correlation coefficients

## Author(s)

Nicolas Robette

## References

Husson, F., Le, S. and Pages, J. (2010). Exploratory Multivariate Analysis by Example Using R, Chapman and Hall.

## See Also

condesc, dimcontrib, dimeta2, dimtypicality

## Examples

```
# specific MCA on Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# description of the dimensions
dimdescr(mca, limit = 0.1, nperm = 10)
```

dimeta2 Correlation ratios (aka eta-squared) of supplementary variables

## Description

Computes correlation ratios (also known as eta-squared) for a list of supplementary variables of a MCA.

## Usage

dimeta2 (resmca, vars, $\operatorname{dim}=c(1,2))$

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
vars a data frame of supplementary variables
dim the axes for which eta2 are computed. Default is $\mathrm{c}(1,2)$

## Value

Returns a data frame with supplementary variables as rows and MCA axes as columns.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

dimdescr, dimcontrib, dimtypicality

## Examples

```
# specific MCA on Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# correlation ratios
dimeta2(mca, Music[, c("Gender", "Age")])
```

dimtypicality Typicality tests for supplementary variables

## Description

Computes typicality tests for a list of supplementary variables of a MCA.

## Usage

dimtypicality(resmca, vars, dim = $c(1,2)$, max.pval $=1)$

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
vars a data frame of supplementary variables
dim the axes for which typicality tests are computed. Default is $c(1,2)$
max.pval only categories with a p-value lower or equal to max.pval are displayed. If 1 (default), all categories are displayed

## Value

Returns a list of data frames giving the typicality test statistics and p-values of the supplementary categories for the different axes.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

dimdescr, dimeta2, dimcontrib

## Examples

\# specific MCA on Music example data set data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
\# typicality tests for gender and age
dimtypicality(mca, Music[, c("Gender", "Age")])

```
dist.chi2 Chi-squared distance
```


## Description

Computes the chi-squared distance between the rows of a data frame of factors.

## Usage

dist.chi2(X)

## Arguments

X data frame. All variables should be factors.

## Details

This function is adapted from chi2Dist function in ExPosition package.

## Value

A symmetrical matrix of distances

## Author(s)

Nicolas Robette

## Examples

```
data(Music)
d <- dist.chi2(Music[,1:5])
# a short piece of the distance matrix
d[1:3, 1:3]
```

    flip.mca Flips the coordinates
    
## Description

Flips the coordinates of the individuals and the categories on one or more dimensions of a MCA.

## Usage

flip.mca(resmca, dim = 1)

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
dim numerical vector of the dimensions for which the coordinates are flipped. By default, only the first dimension is flipped

## Value

Returns an object of the same class as resmca

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables, ggcloud_indiv

## Examples

\# MCA of Music example data set
data(Music)
mca <- speMCA(Music[,1:5])
ggcloud_variables(mca, legend = "none")
\# Flips dimensions 1 and 2
flipped_mca <- flip.mca(mca, dim $=c(1,2))$
ggcloud_variables(flipped_mca, legend = "none")

```
getindexcat Names of the categories in a data frame
```


## Description

Returns a vector of names corresponding the the categories in a data frame exclusively composed of categorical variables.

## Usage

getindexcat(data)

## Arguments

data data frame of categorical variables

## Details

This function may be useful prior to a specific MCA, to identify the indexes of the 'junk' categories to exclude.

## Value

Returns a character vector with the names of the categories of the variables in the data frame

## Author(s)

Nicolas Robette

## See Also

ijunk, speMCA, csMCA

## Examples

```
data(Music)
getindexcat(Music[,1:5])
mca <- speMCA(Music[,1:5], excl = c(3,6,9,12,15))
```

ggadd_attractions Plot of attractions between categories

## Description

Adds attractions between categories, as measured by phi coefficients or percentages of maximum deviation (PEM), by plotting segments onto a MCA cloud of variables.

## Usage

ggadd_attractions(p, resmca, axes $=c(1,2)$, measure $=" p h i ", ~ m i n . a s s o=0.3$, col.segment = "lightgray", col.text = "black", text.size = 3)

## Arguments

p
resmca
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
measure character string. The measure for attractions: "phi" (default) for phi coefficients, "pem" for percentages of maximum deviation (PEM).
min. asso numerical value ranging from 0 to 1 . The minimal attraction value for segments to be plotted. Default is 0.3 .
col.segment
Character string with the color of the segments. Default is lightgray.
col.text
text.size
ggplot2 object with the cloud of variables
resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA.
lue
a ggplot2 object

## Author(s)

Nicolas Robette

## References

Cibois, Philippe. Les méthodes d'analyse d'enquêtes. Nouvelle édition [en ligne]. Lyon: ENS Éditions, 2014. [http://books.openedition.org/enseditions/1443](http://books.openedition.org/enseditions/1443)

## See Also

ggcloud_variables

## Examples

```
# specific MCA on Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
            "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
            "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# Plots attractions
p <- ggcloud_variables(mca, col="white", legend="none")
ggadd_attractions(p, mca, measure="phi", min.asso=0.1)
```

ggadd_chulls Convex hulls for a categorical supplementary variable

## Description

Adds convex hulls for a categorical variable to a MCA cloud of individuals.

## Usage

ggadd_chulls(p, resmca, var, sel = 1:nlevels(var), axes = c(1,2), prop $=1$, alpha = 0.2, label = TRUE, label.size = 5, legend = "right")

## Arguments

p
ggplot2 object with the cloud of individuals
resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
var Factor. The categorical variable used to plot chulls.
sel numeric vector of indexes of the categories to plot (by default, ellipses are plotted for every categories)
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
prop proportion of all the points to be included in the hull (default is 1).
alpha Numerical value from 0 to 1. Transparency of the polygon's fill. Default is O. 2
label Logical. Should the labels of the categories be plotted at the center of chulls ? Default is TRUE.
label.size $\quad$ Size of the labels of the categories at the center of chulls. Default is 5.
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Value

a ggplot2 object

## Note

Chulls are colored according to the categories of the variable, using the default ggplot2 palette. The palette can be customized using any scale_color_* and scale_fill_* functions, such as scale_color_brewer() and scale_fill_brewer(), scale_color_grey() and scale_fill_grey(), or scale_color_manual() and scale_fill_manual().

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

```
ggcloud_indiv, ggadd_supvar,ggadd_supvars, ggadd_kellipses, ggadd_ellipses,ggadd_interaction,
```

ggsmoothed_supvar, ggadd_corr, ggadd_density

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
    "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
    "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# hierarchical clustering
# and partition of the individuals into 3 clusters
d <- dist(mca$ind$coord[, c(1,2)])
hca <- hclust(d, "ward.D2")
cluster <- factor(cutree(hca, 3))
# cloud of individuals
# with convex hulls for the clusters.
p <- ggcloud_indiv(mca, col = "black")
ggadd_chulls(p, mca, cluster)
```


## Description

Adds a heatmap representing the correlation coefficients to a MCA cloud of individuals, for a numerical supplementary variable or one category of a categorical supplementary variable.

## Usage

ggadd_corr(p, resmca, var, cat = levels(var)[1], axes = c(1,2), xbins = 20, ybins = 20, min.n = 1, pal = "RdYlBu", limits = NULL, legend = "right")

## Arguments

p
ggplot2 object with the cloud of variables
resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
var factor or numerical vector. The supplementary variable used for the heatmap.
cat character string. The category of var to plot (by default, the first level of var is plotted). Only used if var is a factor.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
xbins integer. Number of bins in the x axis. Default is 20.
ybins integer. Number of bins in the y axis. Default is 20.
min.n integer. Minimal number of points for a tile to be drawn. By default, every tiles are drawn.
pal character string. Name of a (preferably diverging) palette from the RColorBrewer package. Default is "RdYlBu".
limits numerical vector of length 2. Lower and upper limits of the correlation coefficients for the color scale. Should be centered around 0 for a better view of under/over-representations (for example $c(-0.2,0.2)$ ). By default, the maximal absolute value of the correlation coefficients is used.
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Details

For each tile of the heatmap, a correlation coefficient is computed between the supplementary variable and the fact of belonging to the tile. This gives a view of the under/over-representation of the supplementary variable according to the position in the cloud of individuals.

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables, ggadd_supvar, ggadd_supvars, ggadd_kellipses, ggadd_ellipses, ggadd_interaction, ggsmoothed_supvar, ggadd_chulls, ggadd_density

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
    "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
    "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# correlation heatmap for Age = 50+
p <- ggcloud_indiv(mca, col = "lightgrey")
ggadd_corr(p, mca, var = Taste$Age, cat = "50+", xbins = 10, ybins = 10)
```

```
ggadd_density Density plot of a supplementary variable
```


## Description

For a given category of a supplementary variable, adds a layer representing the density of points to the cloud of individuals, either with contours or areas.

## Usage

ggadd_density(p, resmca, var, cat = levels(var)[1], axes = c(1,2), density = "contour", col.contour = "darkred", pal.area = "viridis", alpha.area $=0.2$, ellipse $=$ FALSE)

## Arguments

p
ggplot2 object with the cloud of variables
resmca
var
object of class MCA, speMCA, csMCA, stMCA or multiMCA
factor or numerical vector. The supplementary variable to be plotted.

| cat | character string. The category of var to plot (by default, the first level of var is <br> plotted). Only used if var is a factor. |
| :--- | :--- |
| axes | numeric vector of length 2, specifying the components (axes) to plot. Default is <br> $c(1,2)$. |
| density | If "contour" (default), density is plotted with contours. If "area", density is <br> plotted with areas. <br> character string. The color of the contours. |
| col.contour | character string. The name of a viridis palette for areas. |
| pal.area | numeric. Transparency of the areas. Default is 0.2. |
| alpha.area | logical. If TRUE, a concentration ellipse is added. |
| ellipse |  |

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_indiv, ggadd_supvar, ggadd_supvars, ggadd_kellipses, ggadd_ellipses, ggadd_interaction, ggsmoothed_supvar, ggadd_chulls, ggadd_corr

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
    "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
    "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
p <- ggcloud_indiv(mca, col='lightgrey')
# density plot for Age = 50+ (with contours)
ggadd_density(p, mca, var = Taste$Age, cat = "50+")
# density plot for Age = 50+ (with contours)
ggadd_density(p, mca, var = Taste$Age, cat = "50+", density = "area")
```

```
ggadd_ellipses Confidence ellipses
```


## Description

Adds confidence ellipses for a categorical variable to a MCA cloud of individuals

## Usage

ggadd_ellipses(p, resmca, var, sel = 1:nlevels(var), axes = c(1,2), level $=0.05$, label $=$ TRUE, label.size $=3$, size $=0.5$, points $=$ TRUE, legend = "right")

## Arguments

p ggplot2 object with the cloud of individuals
resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
var Factor. The categorical variable used to plot ellipses.
sel numeric vector of indexes of the categories to plot (by default, ellipses are plotted for every categories)
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
level The level at which to draw an ellipse (see stat_ellipse). Default is 0.05 , which means 95 percents confidence ellipses are plotted.
label Logical. Should the labels of the categories be plotted at the center of ellipses ? Default is TRUE.
label.size $\quad$ Size of the labels of the categories at the center of ellipses. Default is 3 .
size $\quad$ Size of the lines of the ellipses. Default is 0.5 .
points If TRUE (default), the points are coloured according to their subcloud.
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Details

A confidence ellipse aims at measuring how the "true" mean point of a category differs from its observed mean point. This is achieved by constructing a confidence zone around the observed mean point. If we choose a conventional level alpha (e.g. 0.05 ), a ( $1-$ alpha) (e.g. 95 percents) confidence zone is defined as the set of possible mean points that are not significantly different from the observed mean point.

## Value

a ggplot2 object

## Note

Ellipses are colored according to the categories of the variable, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_indiv, ggadd_supvar, ggadd_supvars, ggadd_kellipses, ggadd_density, ggadd_interaction, ggsmoothed_supvar, ggadd_chulls, ggadd_corr

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# confidence ellipses for Age
p <- ggcloud_indiv(mca, col = "lightgrey")
ggadd_ellipses(p, mca, Music$Age)
```

ggadd_interaction Plot of interactions between two categorical supplementary variables

## Description

Adds the interactions between two categorical supplementary variables to a MCA cloud of variables

## Usage

ggadd_interaction(p, resmca, v1, v2, sel1 = 1:nlevels(v1), sel2 = 1:nlevels(v2), axes $=c(1,2)$, textsize $=5$, legend $=$ "right")

## Arguments

p
resmca
v1
v2 Factor. The second categorical supplementary variable.
sel1 Numeric vector of indexes of the categories of the first supplementary variable to be used in interaction. By default, every categories are used.
sel2 Numeric vector of indexes of the categories of the second supplementary variable to be used in interaction. By default, every categories are used.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
textsize $\quad$ Size of the labels of categories. Default is 5 .
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Value

a ggplot2 object

## Note

Lines and labels are colored according to the variables, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables, ggadd_supvar, ggadd_supvars, ggadd_kellipses, ggadd_ellipses, ggadd_corr, ggsmoothed_supvar, ggadd_chulls, ggadd_density

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
    "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
    "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# interaction between Gender and Age
p <- ggcloud_variables(mca, col = "lightgrey", shapes = FALSE)
ggadd_interaction(p, mca, Taste$Gender, Taste$Age)
```

ggadd_kellipses Concentration ellipses and $k$-inertia ellipses

## Description

Adds concentration ellipses and other kinds of k-inertia ellipses for a categorical variable to a MCA cloud of individuals.

## Usage

ggadd_kellipses( $p$, resmca, var, sel = 1:nlevels(var), axes = c(1,2), kappa $=2$, label $=$ TRUE, label.size $=3$, size $=0.5$, points $=$ TRUE, legend = "right")

## Arguments

p
resmca
var Factor. The categorical variable used to plot ellipses.
sel numeric vector of indexes of the categories to plot (by default, ellipses are plotted for every categories)
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
kappa numeric. The kappa value (i.e. "index") of the inertia ellipses. By default, kappa $=2$, which means that concentration ellipses are plotted.
label Logical. Should the labels of the categories be plotted at the center of ellipses ? Default is TRUE.
label.size Size of the labels of the categories at the center of ellipses. Default is 3 .
size $\quad$ Size of the lines of the ellipses. Default is 0.5 .
points If TRUE (default), the points are coloured according to their subcloud.
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Details

If kappa=2, ellipses are called "concentration" ellipses and, for a normally shaped subcloud, contain 86.47 percents of the points of the subcloud. If kappa $=1$, ellipses are "indicator" ellipses and contain 39.35 percents of the points of the subcloud. If kappa $=1.177$, ellipses are "median" ellipses and contain 50 percents of the points of the subcloud. This function has to be used after the cloud of individuals has been drawn.

## Value

a ggplot2 object

## Note

Ellipses are colored according to the categories of the variable, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_indiv, ggadd_supvar, ggadd_supvars, ggadd_ellipses, ggadd_density, ggadd_interaction, ggsmoothed_supvar, ggadd_chulls, ggadd_corr

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# concentration ellipses for Age
p <- ggcloud_indiv(mca, col = "lightgrey")
ggadd_ellipses(p, mca, Music$Age)
```


## Description

Adds supplementary individuals to a MCA cloud of the individuals

## Usage

ggadd_supind(p, resmca, dfsup, axes $=c(1,2)$,
col = "black", textsize = 5, pointsize = 2)

## Arguments

p
resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA.
dfsup data frame with the supplementary individuals. It must have the same factors as the data frame used as input for the initial MCA.
axes numeric vector of length 2, specifying the dimensions (axes) to plot (default is $\mathrm{c}(1,2))$
col color for the labels and points of the individuals (default is black)
textsize Size of the labels of the individuals. Default is 5.
pointsize Size of the points of the individuals. If NULL, only labels are plotted. Default is 2 .

## Details

The function uses the row names of dfsup as labels for the individuals.

## Author(s)

Nicolas Robette

## See Also

supind, ggcloud_indiv

## Examples

```
# specific MCA of Music example data set
data(Music)
rownames(Music) <- paste0("i", 1:nrow(Music))
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# adds individuals 1, 20 and 300 as supplementary individuals
# onto the cloud of individuals
p <- ggcloud_indiv(mca, col = "lightgrey")
ggadd_supind(p, mca, Music[c(1,20,300), 1:5])
```


## Description

Adds a categorical supplementary variable to a MCA cloud of variables.

## Usage

```
ggadd_supvar(p, resmca, var, sel = 1:nlevels(var), axes = c(1,2),
col = "black", shape = 1, prop = NULL, textsize = 3, shapesize = 6,
segment = FALSE, vname = NULL)
```


## Arguments

p
resmca
var Factor. The categorical supplementary variable. It does not need to have been used at the MCA step.
sel Numeric vector of indexes of the categories of the supplementary variable to be added to the plot. By default, labels are plotted for every categories.
numeric vector of length 2 , specifying the components (axes) to plot. Default is $c(1,2)$.
col Character. Color of the shapes and labels of the categories. Default is black.
shape Symbol to be used in addition the the labels of categories (default is 1). If NULL, only labels are plotted.
prop If NULL, the size of the labels (if shape=NULL) or the shapes (otherwise) is constant. If ' $n$ ', the size is proportional the the weights of categories; if 'vtest 1 ', the size is proportional to the test values of the categories on the first dimension of the plot; if 'vtest2', the size is proportional to the test values of the categories on the second dimension of the plot; if ' $\cos 1$ ', the size is proportional to the cosines of the categories on the first dimension of the plot; if 'cos2', the size is proportional to the cosines of the categories on the second dimension of the plot; if ' $\cos 12$ ', the size is proportional to the total cosines of the categories on the two dimensions of the plot.
textsize Size of the labels of categories if shape is not NULL, or if shape=NULL and prop=NULL. Default is 3 .
shapesize Size of the shapes if prop=NULL, maximum size of the shapes in other cases. Default is 6 .
segment Logical. Should one add lines between categories? Default is FALSE.
vname A character string to be used as a prefix for the labels of the categories. If NULL (default), no prefix is added.

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables, ggadd_supvars, ggadd_ellipses, ggadd_kellipses, ggadd_density, ggadd_interaction, ggsmoothed_supvar, ggadd_chulls, ggadd_corr

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# adds Age as a supplementary variable
# onto the cloud of variables
p <- ggcloud_variables(mca, col = "lightgrey", shapes = FALSE)
ggadd_supvar(p, mca, Music$Age, segment = TRUE)
```

    ggadd_supvars Plot of categorical supplementary variables
    
## Description

Adds categorical supplementary variables to a MCA cloud of variables.

## Usage

```
ggadd_supvars(p, resmca, vars, excl = NULL, points = "all", min.cos2 = 0.1,
axes = c(1,2), col = NULL,
shapes = FALSE, prop = NULL, textsize = 3, shapesize = 6,
vlab = TRUE, vname = NULL,
force = 1, max.overlaps = Inf)
```


## Arguments

| p | ggplot2 object with the cloud of variables |
| :--- | :--- |
| resmca | object of class MCA, speMCA, csMCA, stMCA or multiMCA. |
| vars | A data frame of categorical supplementary variables. All these variables should |
| be factors. |  |
| character vector of supplementary categories to exclude from the plot, speci- |  |
| fied in the form "namevariable.namecategory" (for instance "Gender.Men"). If |  |
| NULL (default), all the supplementary categories are plotted. |  |
| character string. If 'all' all categories are plotted (default); if 'besth' only those |  |
| with a minimum squared cosine on horizontal axis are plotted; if 'bestv' only |  |
| those with a minimum squared cosine on vertical axis are plotted; if 'besthv' |  |
| only those with a minimum squared cosine on horizontal or vertical axis are |  |
| plotted; if 'best' only those with a minimum squared cosine on the plane are |  |
| plotted. |  |

## Value

a ggplot2 object

## Note

Shapes and labels are colored according to the categories of the variable, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables, ggadd_supvar, ggadd_ellipses, ggadd_kellipses, ggadd_density, ggadd_interaction, ggsmoothed_supvar, ggadd_chulls, ggadd_corr

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# adds several supplementary variables
# onto the cloud of variables
p <- ggcloud_variables(mca, col = "lightgrey", shapes = FALSE)
ggadd_supvars(p, mca, Music[, c("Gender","Age")])
# the same, excluding men
ggadd_supvars(p, mca, Music[, c("Gender","Age")], excl = "Gender.Men")
# the same, keeping only categories
# with cos2 >= 0.001 for dimension 1
ggadd_supvars(p, mca, Music[, c("Gender","Age")], points = "besth", min.cos2 = 0.001)
```

ggaxis_variables

## Description

Plots variables on a single axis of a Multiple Correspondence Analysis. Variables can be active or supplementary.

## Usage

```
    ggaxis_variables(resmca, var = NULL, axis = 1, prop = NULL,
    underline = FALSE, col = NULL, vlab = TRUE)
```


## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA.
var If NULL (default), all the active variables of the MCA are plotted. If a character string, the named active variables of the MCA is plotted. If a factor, it is plotted as a supplementary variable.
axis numeric value. The MCA axis to plot. Default is 1 .
prop If NULL (default), the size of the labels is constant. If "freq", the size is proportional to the weights of categories. If "ctr", it's proportional to the contributions of categories (only used for active variables). If "cos 2 ", it's proportional to the squared cosines of the categories. If "pval", it's proportional to 1 minus the p-values of typicality tests (only used for supplementary variables). If "cor", it's proportional to the point biserial correlation of the categories (only used for supplementary variables).
underline logical. If TRUE, the labels of the categories with contributions above average are underlined. Default is FALSE. Only used for active variables.
col character string. Color name for the labels of the categories. If NULL and var=NULL, the default palette of ggplot2 is used, with one color per variable. If NULL and var is not NULL, labels are black.
vlab Logical. Should the variable names be used as a prefix for the labels of the categories. Default is TRUE.

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
        "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
        "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# plots all the active categories on axis 1
ggaxis_variables(mca)
# the same with other plotting options
ggaxis_variables(mca, prop = "freq", underline = TRUE, col = "black")
# plots Active variable Classical on axis 1
ggaxis_variables(mca, var = "Classical", axis = 1, prop = "ctr", underline = TRUE)
# plots supplementary variable Educ on axis 1
ggaxis_variables(mca, var = Taste$Educ, axis = 1, prop = "pval")
```

ggbootvalid_supvars Ellipses of bootstrap validation (supplementary variables)

## Description

Ellipses for bootstrap validation of MCA, through the computation of the coordinates of supplementary variables for bootstrap replications of the data.

## Usage

$$
\begin{aligned}
& \text { ggbootvalid_supvars(resmca, vars = NULL, axes }=c(1,2), \mathrm{K}=30, \\
& \\
& \text { ellipse }=" \text { norm", level }=0.95, \\
& \\
& \text { col }=\text { NULL, active }=\text { FALSE, legend = "right") }
\end{aligned}
$$

## Arguments

| resmca | object of class speMCA. |
| :---: | :---: |
| vars | A data frame of categorical supplementary variables. All these variables should be factors. |
| axes | numeric vector of length 2 , specifying the components (axes) to plot. Default is $c(1,2)$. |
| K | integer. Number of bootstrap replications (default is 30). |
| ellipse | character string. The type of ellipse. The default "norm" assumes a multivariate normal distribution, " t " assumes a multivariate t -distribution, and "euclid" draws a circle with the radius equal to level, representing the euclidean distance from the center. |
| level | numerical value. The level at which to draw an ellipse, or, if ellipse="euclid", the radius of the circle to be drawn. |
| col | Character string. Color name for the ellipses and labels of the categories. If NULL (default), the default ggplot2 palette is used, with one color per variable. |

active logical. If TRUE, the labels of active variables are added to the plot in lightgray. Default is FALSE.
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Details

The bootstrap technique is used here as an internal (and non-parametric) validation procedure of the results of a multiple correspondence analysis. For supplementary variables, only partial bootstrap is possible. The partial bootstrap does not compute new MCAs: it projects bootstrap replications of the initial data as supplementary elements of the MCA. See references for more details.
The default parameters for ellipses assume a multivariate normal distribution drawn at level 0.95.

## Value <br> a ggplot2 object

## Note

If col argument is NULL, ellipses and labels are colored according to the variables, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Nicolas Robette

## References

Lebart L. (2006). "Validation Techniques in Multiple Correspondence Analysis". In M. Greenacre et J. Blasius (eds), Multiple Correspondence Analysis and related techniques, Chapman and Hall/CRC, p.179-196.

Lebart L. (2007). "Which bootstrap for principal axes methods?". In P. Brito et al. (eds), Selected Contributions in Data Analysis and Classification, Springer, p.581-588.

## See Also

bootvalid_supvars, ggbootvalid_variables

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
            "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
            "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# bootstrap validation ellipses
# for three supplementary variables
sup <- Taste[,c("Gender", "Age", "Educ")]
```

ggbootvalid_supvars(mca, sup)
ggbootvalid_variables Ellipses of bootstrap validation (active variables)

## Description

Ellipses for bootstrap validation of MCA, through the computation of the coordinates of active variables for bootstrap replications of the data.

## Usage

ggbootvalid_variables(resmca, axes = c(1,2), type = "partial", K = 30, ellipse = "norm", level = 0.95, col = NULL, legend = "right")

## Arguments

resmca object of class speMCA.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $\mathrm{c}(1,2)$.
type character string. Can be "partial", "total1", "total2" or "total3" (see details). Default is "partial".
K integer. Number of bootstrap replications (default is 30).
ellipse character string. The type of ellipse. The default "norm" assumes a multivariate normal distribution, "t" assumes a multivariate t-distribution, and "euclid" draws a circle with the radius equal to level, representing the euclidean distance from the center.
level numerical value. The level at which to draw an ellipse, or, if ellipse="euclid", the radius of the circle to be drawn.
col Character string. Color name for the ellipses and labels of the categories. If NULL (default), the default ggplot2 palette is used, with one color per variable.
legend the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right.

## Details

The bootstrap technique is used here as an internal (and non-parametric) validation procedure of the results of a multiple correspondence analysis. Following the work of Lebart, several methods are proposed. The total bootstrap uses new MCAs computed from bootstrap replications of the initial data. In the type 1 bootstrap (type = "total1"), the sign of the coordinates is corrected if necessary (the direction of the axes of an ACM being arbitrary). In type 2 (type = "total2"), the order of the axes and the sign of the coordinates are corrected if necessary. In type 3 (type = "total3"), a procrustean rotation is used to find the best superposition between the initial axes and the replicated axes. The partial bootstrap (type $=$ "partial") does not compute new MCAs: it projects bootstrap
replications of the initial data as supplementary elements of the MCA. It gives a more optimistic view of the stability of the results than the total bootstrap. It is also faster. See references for more details, pros and cons of the various types, etc.

The default parameters for ellipses assume a multivariate normal distribution drawn at level 0.95.

## Value

a ggplot2 object

## Note

If col argument is NULL, ellipses and labels are colored according to the variables, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Nicolas Robette

## References

Lebart L. (2006). "Validation Techniques in Multiple Correspondence Analysis". In M. Greenacre et J. Blasius (eds), Multiple Correspondence Analysis and related techniques, Chapman and Hall/CRC, p.179-196.

Lebart L. (2007). "Which bootstrap for principal axes methods?". In P. Brito et al. (eds), Selected Contributions in Data Analysis and Classification, Springer, p.581-588.

## See Also

```
bootvalid_variables,ggbootvalid_supvars
```


## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
                            "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
                            "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# bootstrap validation ellipses for active variables
ggbootvalid_variables(mca, type = "partial", K = 5)
```


## Description

Plots a Multiple Correspondence Analysis cloud of individuals.

## Usage

ggcloud_indiv(resmca, type = "i", points = "all", axes = $c(1,2)$,
col = "dodgerblue4", point.size = 0.5, alpha = 0.6,
repel = FALSE, text.size $=2$,
density = NULL, col.contour = "darkred", hex.bins = 50, hex.pal = "viridis")

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
type If 'i', points are plotted. If 'inames', labels of individuals are plotted.
points character string. If 'all' all points are plotted (default). If 'besth' only those who contribute most to horizontal axis are plotted. If 'bestv' only those who contribute most to vertical axis are plotted. If 'besthv' only those who contribute most to horizontal or vertical axis are plotted. If 'best' only those who contribute most to the plane are plotted.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $c(1,2)$.
col If a factor, points or labels are colored according to their category regarding this factor. If a string with color name, every points or labels have the same color. Default is "dodgerblue4".
point.size Size of the points of individuals. Default is 0.5 .
alpha Transparency of the points or labels of individuals. Default is 0.6.
repel Logical. When type="inames"", should labels of individuals be repeled ? Default is FALSE.
text.size $\quad$ Size of the labels of individuals. Default is 2.
density If NULL (default), no density layer is added. If "contour", density is plotted with contours. If "hex", density is plotted with hexagon bins.
col. contour character string. The color of the contours. Only used if density="contour".
hex.bins integer. The number of bins in both vertical and horizontal directions. Only used if density="hex".
hex.pal character string. The name of a viridis palette for hexagon bins. Only used if density="hex".

## Details

Sometimes the dots are too many and overlap. It is then difficult to get an accurate idea of the distribution of the cloud of individuals. The density argument allows you to add an additional layer to represent the density of points in the plane, in the form of contours or hexagonal areas.

## Value

a ggplot2 object

## Note

If col argument is a factor, points or labels are colored according to the categories of the factor, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().

## Author(s)

Anton Perdoncin, Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_variables

## Examples

```
# specific MCA of Taste example data set
data(Taste)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
            "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
            "Musical.NA")
mca <- speMCA(Taste[,1:11], excl = junk)
# cloud of individuals
ggcloud_indiv(mca)
# points are colored according to gender
ggcloud_indiv(mca, col=Taste$Gender)
# a density layer of contours is added
ggcloud_indiv(mca, density = "contour")
# a density layer of hexagon bins is added
ggcloud_indiv(mca, density = "hex", hex.bin = 10)
```


## Description

Plots a Multiple Correspondence Analysis cloud of variables.

## Usage

```
ggcloud_variables(resmca, axes = c(1,2), points = "all",
min.ctr = NULL, max.pval = 0.01, face = "pp",
shapes = TRUE, prop = NULL, textsize = 3, shapesize = 3,
col = NULL, col.by.group = TRUE, alpha = 1,
segment.alpha = 0.5, vlab = TRUE, sep = ".", legend = "right",
force = 1, max.overlaps = Inf)
```


## Arguments

| resmca | object of class MCA, speMCA, csMCA, stMCA or multiMCA. |
| :--- | :--- |
| axes | numeric vector of length 2, specifying the components (axes) to plot. Default is <br> c(1,2). <br> points <br> character string. If 'all' all categories are plotted (default); if 'besth' only those <br> who contribute most to horizontal axis are plotted; if 'bestv' only those who <br> contribute most to vertical axis are plotted; if 'besthv' only those who contribute <br> most to horizontal or vertical axis are plotted; if 'best' only those who contribute <br> most to the plane are plotted. |
| min.ctr | Numerical value between 0 and 100. The minimum contribution (in percent) <br> for a category to be displayed if the points argument is equal to "best", "besth" <br> or "bestv" and resmca is of type MCA, speMCA or csMCA. If NULL (default), <br> only the categories that contribute more than the average (i.e. 100 / number of <br> modalities) are displayed. |
| max.pval | Numerical value between 0 and 100. The maximal p-value derived from test- <br> values for a category to be displayed if the points argument is equal to "best", <br> "besth" or "bestv" and resmca is of type stMCA or multimCA. <br> character string. Changes the face of the category labels when their contribution |
| is greater than min.ctr. The first letter refers to the first represented axis, the |  |


| prop | If NULL, the size of the labels (if shapes=FALSE) or the shapes (if shapes=TRUE) is constant. If ' $n$ ', the size is proportional the the weights of categories; if ' ctr 1 ', the size is proportional to the contributions of the categories on the first dimension of the plot; if 'ctr2', the size is proportional to the contributions of the categories on the second dimension of the plot; if ' 'tr12', the size is proportional to the contributions of the categories on the plane ; if 'ctr.cloud', the size is proportional to the total contributions of the categories on the whole cloud; if ' $\cos ^{1}$ ', the size is proportional to the quality of representation (squared cosines) of the categories on the first dimension of the plot; if 'cos2', the size is proportional to the quality of representation of the categories on the second dimension of the plot; if ' $\cos 12$ ', the size is proportional to the quality of representation of the categories on the plane; if 'vtest1', the size is proportional to the testvalues of the categories on the first dimension of the plot; if 'vtest2', the size is proportional to the test-values of the categories on the second dimension of the plot. |
| :---: | :---: |
| textsize | Size of the labels of categories if shapes=TRUE, or if shapes=FALSE and prop=NULL. Default is 3 . |
| shapesize | Size if the shapes of categories if shapes=TRUE and prop=FALSE. Default is 3 . |
| col | Character string. Color name for the shapes and labels of the categories. If NULL (default), the default ggplot2 palette is used, with one color per variable. |
| col.by.group | Logical. If resmca is of type multimCA, categories are colored by group from the MFA if TRUE (default) and by variable if FALSE. |
| alpha | Transparency of the shapes and labels of categories. Default is 1. |
| segment.alpha | Transparency of the line segment beside labels of categories. Default is 0.5 . |
| vlab | Logical. Should the variable names be used as a prefix for the labels of the categories. Default is TRUE. |
| sep | Character string used as a separator if vlab=TRUE. |
| legend | the position of legends ("none", "left", "right", "bottom", "top", or two-element numeric vector). Default is right. |
| force | Force of repulsion between overlapping text labels. Defaults to 1 . If 0 , labels are not repelled at all. |
| max.overlaps | Exclude text labels that overlap too many things. Defaults to Inf, which means no labels are excluded. |

## Value

a ggplot2 object

## Note

If col argument is NULL, shapes or labels are colored according to the variables, using the default ggplot2 palette. The palette can be customized using any scale_color_* function, such as scale_color_brewer(), scale_color_grey() or scale_color_manual().
If resmca is of type stMCA or multimCA and points is not equal to "all", test-values are used instead of contributions (which are not available for these MCA variants) to select the most important categories ; if points is equal to best, only categories with high test-values for horizontal axis or vertical axis are plotted.

## Author(s)

Anton Perdoncin, Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggcloud_indiv

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# cloud of variables
ggcloud_variables(mca)
# cloud of variables with only categories contributing the most
ggcloud_variables(mca, points = "best", prop = "n")
# cloud of variables with other plotting options
ggcloud_variables(mca, shapes = FALSE, legend = "none",
col = "black", face = "ui")
```

```
ggeta2_variables eta-squared plot
```


## Description

Plots the eta-squared (squared correlation ratios) of the active variables of a MCA.

## Usage

ggeta2_variables(resmca, axes = c(1,2))

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $c(1,2)$.

## Details

This plot was proposed by Escofier and Pagès (2008) under the name "carré des liaisons", i.e. square of relationships, using correlation ratios to measure these relationships. Eta-squared (i.e. correlation ratio) is a measure of global association between a continuous variable and a categorical variable : it measures the share of variance of the continuous variables "explained" by the categorical variable. Here, it is used to plot the association between the active variables and the axes of the MCA cloud.

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Escofier B. and Pagès J., 2008, Analyses factorielles simples et multiples, Dunod.

## See Also

ggcloud_variables, ggadd_attractions

## Examples

```
data(Music)
junk <- c("FrenchPop.NA","Rap.NA","Jazz.NA","Classical.NA","Rock.NA")
mca <- speMCA(Music[,1:5], excl = junk)
ggeta2_variables(mca)
```

ggsmoothed_supvar Plots the density a supplementary variable

## Description

Plots the density of a supplementary variable in a MCA space, using a grid, smoothing and interpolation (via inverse distance weighting.)

## Usage

```
ggsmoothed_supvar(resmca, var, cat, axes = c(1,2),
    center = FALSE, scale = FALSE,
    nc = c(20, 20), power = 2,
    limits = NULL, pal = "RdBu")
```


## Arguments

resmca object of class PCA, MCA, speMCA, csMCA, stMCA or multimCA.
var factor or numeric vector. The supplementary variable to be plotted.
cat character string. If var is a factor, the name of the level of the supplementary variable to be plotted.
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $c(1,2)$.
center logical. Whether the supplementary variable should be centered or not. Default is FALSE.
scale logical. Whether the supplementary variable should be scaled to unit variance or not. Default is FALSE.
nc integer vector of length 2. Number of grid cells in $x$ and $y$ direction (columns, rows).
power numerical value. The power to use in weight calculation for inverse distance weighting. Default is 2 .
limits numerical vector of length 2. Lower and upper limit of the scale for the supplementary variable.
pal character string. Name of a (preferably diverging) palette from the RColorBrewer package. Default is "RdBu".

## Details

The construction of the plot takes place in several steps. First, the two-dimensional MCA space is cut into a grid of hexagonal cells. Then, for each cell, the average value of the supplementary variable is calculated for the observations located in that cell (if the variable is numerical), or the proportion of observations belonging to the category studied (if the variable is categorical). The results are interpolated and smoothed to make the plot easier to read, using the inverse distance weighting technique, which is very common in spatial analysis.
The supplementary variable can be centered beforehand, to represent deviations from the mean (for a numerical variable) or from the mean proportion (for a categorical variable). It can also be scaled to measure deviations in numbers of standard deviations, which can be useful for comparing the results of several supplementary variables.

## Value

a ggplot2 object

## Author(s)

Nicolas Robette

## References

Shepard, Donald (1968). "A two-dimensional interpolation function for irregularly-spaced data". Proceedings of the 1968 ACM National Conference. pp. 517-524. doi:10.1145/800186.810616

## See Also

```
ggadd_supvar,ggadd_supvars,ggadd_kellipses, ggadd_ellipses,ggadd_interaction,ggadd_corr,
ggadd_chulls, ggadd_density
```


## Examples

```
    # specific MCA of Taste example data set
    data(Taste)
    junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA",
        "Comedy.NA", "Crime.NA", "Animation.NA", "SciFi.NA", "Love.NA",
        "Musical.NA")
    mca <- speMCA(Taste[,1:11], excl = junk)
    # density plot for Educ = "High"
    ggsmoothed_supvar(mca, Taste$Educ, "High")
    # centered and scaled density plot for Age
    ggsmoothed_supvar(mca, as.numeric(Taste$Age), center = TRUE, scale = TRUE)
```

    gPCA Generalized Principal Component Analysis
    
## Description

Generalized Principal Component Analysis

## Usage

gPCA(X, row.w = NULL, col.w = NULL, center = FALSE, scale = FALSE, tol = 1e-07)

## Arguments

X
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
col.w numeric vector of column weights. If NULL (default), a vector of 1 for uniform column weights is used.
center logical. If TRUE, variables are centered (default is FALSE).
scale logical. If TRUE, variables are scaled to unit variance (default is FALSE).
tol a tolerance threshold for null eigenvalues (a value less than tol times the first one is considered as null)

## Details

Generalized PCA is basically a PCA with the possibility to specify row weights (i.e. "masses") and variable weights (i.e. the "metric"), and to choose whether to center and scale the variables. This flexibility makes it the building block of many variants of PCA, such as Correspondence Analysis and Multiple Correspondence Analysis.

Generalized PCA is also known as "biweighted PCA", "duality diagram" or "generalized singular value decomposition".

Value
An object of class PCA from FactoMineR package

## Author(s)

Nicolas Robette

## References

Bry X., 1995, Analyses factorielles simples, Economica.
Escofier B. and Pagès J., Analyses factorielles simples et multiples, Dunod (2008).
Escoufier, Y. (1987) The duality diagram : a means of better practical applications In Development in numerical ecology, Legendre, P. \& Legendre, L. (Eds.) NATO advanced Institute, Serie G. Springer Verlag, Berlin, 139-156.

## Examples

```
library(FactoMineR)
data(decathlon)
res <- gPCA(decathlon[,1:10], center = TRUE, scale = TRUE)
plot(res, choix = "var")
```

homog.test

Homogeneity test for a categorical supplementary variable

## Description

From MCA results, computes a homogeneity test between categories of a supplementary variable, i.e. characterizes the homogeneity of several subclouds.

## Usage

homog.test(resmca, var, dim $=c(1,2))$

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
var the categorical supplementary variable. It does not need to have been used at the MCA step.
dim the axes which are described. Default is $\mathrm{c}(1,2)$

## Value

Returns a list of lists, one for each selected dimension in the MCA. Each list has 2 elements :
test.stat The square matrix of test statistics
$p$.values The square matrix of p-values

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

```
supvar, supvars, dimtypicality
```


## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# homogeneity test for variable Age
homog.test(mca, Music$Age)
```

i junk App for junk categories of specific MCA

## Description

This function launches a shiny app to define interactively the junk categories before a specific MCA.

## Usage

ijunk(data, init_junk = NULL)

## Arguments

data data frame of categorical variables to be used as active in a specific MCA
init_junk optional vector of junk categories. Can be a numeric vector indicating the indexes of the junk categories or a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male"). Default is NULL.

## Details

Once the selection of junk categories is interactively done, the function provides the code to use in a script. It also offer the opportunity to select a set of junk categories at once by writing the common suffix of these categories.

## Value

A character vector of junk categories

## Author(s)

Nicolas Robette

## See Also

```
speMCA, csMCA, getindexcat
```


## Examples

```
    ## Not run:
    data(Music)
    ijunk(Music[,1:5])
    # or
    junk <- ijunk(Music[,1:5])
    # To update an existing vector of junk categories
    junk <- ijunk(Music[,1:5], init_junk = c("Rock.NA", "Rap.NA"))
    # and then
    mca <- speMCA(Music[,1:5], excl = junk)
    ## End(Not run)
```

MCAiv
Multiple Correspondence Analysis with Instrumental Variables

## Description

Multiple Correspondence Analysis with Instrumental Variables

## Usage

MCAiv(Y, X, excl = NULL, row.w = NULL, ncp = 5)

## Arguments

$Y \quad$ data frame with only factors
$X \quad$ data frame of instrumental variables, which can be numeric or factors. It must have the same number of rows as Y .
excl numeric vector indicating the indexes of the "junk" categories (default is NULL). See getindexcat or use ijunk interactive function to identify these indexes. It may also be a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male").
row.w Numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp number of dimensions kept in the results (by default 5)

## Details

Multiple Correspondence Analysis with Instrumental Variables consists in three steps: 1. Specific MCA of $Y$, keeping all the dimensions of the space 2. Computation of one linear regression for each dimension in the specific MCA, with individual coordinates as response and all variables in $X$ as explanatory variables. 3. Principal Component Analysis of the set of predicted values from the regressions in 2.
Multiple Correspondence Analysis with Instrumental Variables is also known as "Canonical Correspondence Analysis" or "Constrained Correspondence Analysis".

## Value

An object of class PCA from FactoMineR package, with $Y$ and $X$ as supplementary variables, and an additional item :
ratio the share of inertia explained by the instrumental variables

Note
If there are NAs in $Y$, these NAs will be automatically considered as junk categories. If one desires more flexibility, $Y$ should be recoded to add explicit factor levels for NAs and then excl option may be used to select the junk categories.

## Author(s)

Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

bcMCA, DAQ, bcPCA, DA, PCAiv

## Examples

```
library(FactoMineR)
data(tea)
# MCAIV of tea data
# with age, sex, SPC and Sport as instrumental variables
mcaiv <- MCAiv(tea[,1:18], tea[,19:22])
mcaiv$ratio
plot(mcaiv, choix = "ind", invisible = "ind", col.quali = "black")
```


## Description

Multiple Correspondence Analysis with Orthogonal Instrumental Variables

## Usage

MCAoiv(X, Z, excl = NULL, row.w = NULL, ncp = 5)

## Arguments

$X \quad$ data frame with only factors
Z data frame of instrumental variables, which can be numeric or factors. It must have the same number of rows as $X$.
excl numeric vector indicating the indexes of the "junk" categories (default is NULL). See getindexcat or use ijunk interactive function to identify these indexes. It may also be a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male").
row.w Numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp number of dimensions kept in the results (by default 5)

## Details

Multiple Correspondence Analysis with Orthogonal Instrumental Variables consists in three steps : 1. Specific MCA of $Y$, keeping all the dimensions of the space 2. Computation of one linear regression for each dimension in the specific MCA, with individual coordinates as response and all variables in X as explanatory variables. 3. Principal Component Analysis of the set of residuals from the regressions in 2.

## Value

An object of class PCA from FactoMineR package, with $X$ as supplementary variables, and an additional item :
ratio the share of inertia not explained by the instrumental variables

## Note

If there are NAs in $Y$, these NAs will be automatically considered as junk categories. If one desires more flexibility, $Y$ should be recoded to add explicit factor levels for NAs and then excl option may be used to select the junk categories.
medoids

## Author(s)

Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

wcMCA, wcPCA, PCAoiv

## Examples

```
library(FactoMineR)
data(tea)
mcaoiv <- MCAoiv(tea[,1:18], tea[,19:22])
mcaoiv$ratio
plot(mcaoiv, choix = "ind", invisible = "ind", col.quali = "black")
```

medoids Medoids of clusters

## Description

Computes the medoids of a cluster solution.

## Usage

medoids(D, cl)

## Arguments

D
cl
square distance matrix ( n rows * n columns, i.e. n individuals) or dist object vector with the clustering solution (its length should be n)

## Details

A medoid is a representative object of a cluster whose average dissimilarity to all the objects in the cluster is minimal. Medoids are always members of the data set (contrary to means or centroids).

## Value

Returns a numeric vector with the indexes of medoids.

## Author(s)

Nicolas Robette

## References

Kaufman, L. and Rousseeuw, P.J. (1990). Finding Groups in Data: An Introduction to Cluster Analysis. Wiley, New York.
Anja Struyf, Mia Hubert \& Peter J. Rousseeuw (1996). "Clustering in an Object-Oriented Environment". Journal of Statistical Software.

## See Also

dist, cluster, hclust, cutree, pam

## Examples

\# hierarchical clustering of the Music example data set, \# partition into 3 groups
\# and then computation of the medoids.
data(Music)
temp <- dichotom(Music[,1:5])
d <- dist (temp)
clus <- cutree(hclust(d), 3)
medoids(d, clus)
modif.rate Benzecri's modified rates of variance

## Description

Computes Benzecri's modified rates of variance of a multiple correspondence analysis.

## Usage

```
    modif.rate(resmca)
```


## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA

## Details

As MCA clouds often have a high dimensionality, the variance rates of the first principle axes may be quite low, which makes them hard to interpret. Benzecri (1992, p.412) proposed to use modified rates to better appreciate the relative importance of the principal axes.
multiMCA

## Value

Returns a list of two data frames. The first one is called raw and has 3 variables:

| eigen | eigen values |
| :--- | :--- |
| rate | rates |
| cum.rate | cumulative rates |

The second one is called modif and has 2 variables:
mrate modified rates
cum.mrate cumulative modified rates

## Author(s)

Nicolas Robette

## References

Benzecri J.P., Correspondence analysis handbook, New-York: Dekker (1992).
Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

MCA, speMCA, csMCA

## Examples

```
# MCA of Music' example data set
data(Music)
mca <- speMCA(Music[,1:5])
# modified rates of variance
modif.rate(mca)
```

```
multiMCA Multiple Factor Analysis
```


## Description

Performs Multiple Factor Analysis, drawing on the work of Escofier and Pages (1994). It allows the use of MCA variants (e.g. specific MCA or class specific MCA) as inputs.

## Usage

multiMCA(l_mca, ncp $=5$, compute. $\mathrm{rv}=\mathrm{FALSE}$ )

## Arguments

$\begin{array}{ll}\text { l_mca } & \text { a list of objects of class MCA, speMCA or csMCA } \\ \text { ncp } & \text { number of dimensions kept in the results (default is 5) } \\ \text { compute.rv } & \begin{array}{l}\text { whether RV coefficients should be computed or not (default is FALSE, which } \\ \text { makes the function execute faster) }\end{array}\end{array}$

## Details

This function binds individual coordinates from every MCA in l_mca argument, weights them by the first eigenvalue, and the resulting data frame is used as input for Principal Component Analysis (PCA).

## Value

Returns an object of class multimCA, i.e. a list:
eig a list of numeric vector for eigenvalues, percentage of variance and cumulative percentage of variance
var a list of matrices with results for input MCAs components (coordinates, correlations between variables and axes, squared cosines, contributions)
ind a list of matrices with results for individuals (coordinates, squared cosines, contributions)
call a list with informations about input data
VAR a list of matrices with results for categories and variables in the input MCAs (coordinates, squared cosines, test-values, variances)
my.mca lists the content of the objects in l_mca argument
RV a matrix of RV coefficients

## Author(s)

Nicolas Robette

## References

Escofier, B. and Pages, J. (1994) "Multiple Factor Analysis (AFMULT package)". Computational Statistics and Data Analysis, 18, 121-140.

## See Also

plot.multiMCA, speMCA, csMCA

## Examples

```
data(Taste)
# specific MCA on music variables of Taste example data set
mca1 <- speMCA(Taste[,1:5], excl = c(3,6,9,12,15))
# specific MCA on movie variables of Taste example data set
mca2 <- speMCA(Taste[,6:11], excl = c(3,6,9,12,15,18))
# Multiple Factor Analysis of the two sets of variables
mfa <- multiMCA(list(mca1,mca2))
plot.multiMCA(mfa)
```

Music

Music (data)

## Description

The data concerns tastes for music of a set of 500 individuals. It contains 5 variables of likes for music genres (french pop, rap, rock, jazz and classical), 2 variables about music listening and 2 additional variables (gender and age).

## Usage

data(Music)

## Format

A data frame with 500 observations and the following 7 variables:
FrenchPop factor with levels No, Yes, NA
Rap factor with levels No, Yes, NA
Rock factor with levels No, Yes, NA
Jazz factor with levels No, Yes, NA
Classical factor with levels No, Yes, NA
Gender factor with levels Men, Women
Age factor with levels 15-24, 25-49, 50+
OnlyMus factor with levels Daily, Often, Rare, Never, indicating how often one only listens to music.
Daily is a factor with levels No, Yes indicating if one listens to music every day.

## Details

NA stands for "not available"

## Examples

```
data(Music)
str(Music)
```

nsCA Nonsymmetric Correspondence Analysis

## Description

Nonsymmetric correspondence analysis, for analysing contingency tables with a dependence structure

## Usage

nsCA(X, ncp $=5$, row. sup $=$ NULL, col.sup $=$ NULL, quanti.sup $=$ NULL, quali.sup $=$ NULL, graph $=$ FALSE, axes $=c(1,2)$, row. $w=$ NULL)

## Arguments

$\mathrm{X} \quad$ a data frame or a table with $n$ rows and $p$ columns, i.e. a contingency table. Predictor variable should be in rows and response variable in columns.
ncp number of dimensions kept in the results (by default 5)
row.sup a vector indicating the indexes of the supplementary rows
col.sup a vector indicating the indexes of the supplementary columns
quanti.sup a vector indicating the indexes of the supplementary continuous variables
quali.sup a vector indicating the indexes of the categorical supplementary variables
graph boolean, if TRUE a graph is displayed
axes a length 2 vector specifying the components to plot
row.w an optional row weights (by default, a vector of 1 and each row has a weight equals to its margin); the weights are given only for the active rows

## Details

When dealing with a contingency table with a dependence structure, i.e. when the role of the two variables is not symmetrical but, on the contrary, one can be considered as predicting the other, nonsymmetric correspondence analysis (NSCA) can be used to represent the predictive structure in the table and to assess the predictive power of the predictor variable.
Technically, NSCA is very similar to the standard CA, the main difference being that the columns of the contingency table are not weighted by their rarity (i.e. the inverse of the marginal frequencies).

## Value

An object of class CA from FactoMineR package, with an additional item :
GK.tau Goodman and Kruskal tau

## Note

The code is adapted from the CA function in FactoMineR package.

## Author(s)

Nicolas Robette

## References

Kroonenberg P.M. and Lombardo R., 1999, "Nonsymmetric Correspondence Analysis: A Tool for Analysing Contingency Tables with a Dependence Structure", Multivariate Behavioral Research, 34 (3), 367-396.

## See Also

```
nsca.biplot
```


## Examples

```
data(Music)
# The combination of Gender and Age is the predictor variable
# "Focused" listening to music is the response variable
tab <- with(Music, table(interaction(Gender, Age), OnlyMus))
nsca <- nsCA(tab)
nsca.biplot(nsca)
# Goodman and Kruskal tau
nsca$GK.tau
```

    nsca.biplot Biplot for Nonsymmetric Correspondence Analysis
    
## Description

Biplot for Nonsymmetric correspondence analysis, for analysing contingency tables with a dependence structure

## Usage

nsca.biplot(nsca, axes $=c(1,2))$

## Arguments

nsca an object of class CA created by nsCA() function
axes numeric vector of length 2, specifying the components (axes) to plot. Default is $c(1,2)$.

## Details

The biplots of an NSCA reflect the dependency structure of the contingency table and thus should not be interpreted as the planes of a standard CA. A first principle is that the graph displays the centred row profiles. A second principle is that the relationships between rows and columns are contained in their inner products : the rows are depicted as vectors, also called biplot axes, and the columns are projected on these vectors. If some columns have projections on the row vector far away from the origin, then the row has a comparatively large increase in predictability, and its profile deviates considerably from the marginal one, especially for that column.
For more detailed interpretational guidelines, see Kroonenberg and Lombardo (1999, pp.377-378).

Value
a ggplot2 object

## Author(s)

Nicolas Robette

## References

Kroonenberg P.M. and Lombardo R., 1999, "Nonsymmetric Correspondence Analysis: A Tool for Analysing Contingency Tables with a Dependence Structure", Multivariate Behavioral Research, 34 (3), 367-396.

## See Also

nsCA

## Examples

```
data(Music)
# The combination of Gender and Age is the predictor variable
# "Focused" listening to music is the response variable
tab <- with(Music, table(interaction(Gender, Age), OnlyMus))
nsca <- nsCA(tab)
nsca.biplot(nsca)
# Goodman and Kruskal tau
nsca$GK.tau
```

PCAiv

## Description

Principal Component Analysis with Instrumental Variables

## Usage

PCAiv(Y, X, row.w = NULL, $\mathrm{ncp}=5$ )

## Arguments

$Y$ data frame with only numeric variables
$X \quad$ data frame of instrumental variables, which can be numeric or factors. It must have the same number of rows as Y .
row.w Numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp number of dimensions kept in the results (by default 5)

## Details

Principal Component Analysis with Instrumental Variables consists in two steps: 1. Computation of one linear regression for each variable in $Y$, with this variable as response and all variables in $X$ as explanatory variables. 2. Principal Component Analysis of the set of predicted values from the regressions in 1 ("Y hat").

Principal Component Analysis with Instrumental Variables is also known as "redundancy analysis"

## Value

An object of class PCA from FactoMineR package, with $X$ as supplementary variables, and an additional item :
ratio the share of inertia explained by the instrumental variables

## Author(s)

Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

bcPCA, DA, bcMCA, DAQ, MCAiv

## Examples

```
library(FactoMineR)
data(decathlon)
# PCAiv of decathlon data set
# with Points and Competition as instrumental variables
pcaiv <- PCAiv(decathlon[,1:10], decathlon[,12:13])
pcaiv$ratio
# plot of \code{Y} variables + quantitative instrumental variables (here Points)
plot(pcaiv, choix = "var")
# plot of qualitative instrumental variables (here Competition)
plot(pcaiv, choix = "ind", invisible = "ind", col.quali = "black")
```

PCAoiv Principal Component Analysis with Orthogonal Instrumental Vari-
ables

## Description

Principal Component Analysis with Orthogonal Instrumental Variables

## Usage

PCAoiv(X, Z, row.w = NULL, ncp = 5)

## Arguments

$X \quad$ data frame with only numeric variables
Z data frame of instrumental variables to be "partialled out"", which can be numeric or factors. It must have the same number of rows as $X$.
row.w Numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp number of dimensions kept in the results (by default 5)

## Details

Principal Component Analysis with Orthogonal Instrumental Variables consists in two steps : 1. Computation of one linear regression for each variable in $X$, with this variable as response and all variables in $Z$ as explanatory variables. 2. Principal Component Analysis of the set of residuals from the regressions in 1 .

## Value

An object of class PCA from FactoMineR package, and an additional item :
ratio the share of inertia not explained by the instrumental variables

## Author(s)

Nicolas Robette

## References

Bry X., 1996, Analyses factorielles multiples, Economica.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

wcPCA, wcMCA, MCAoiv

## Examples

```
library(FactoMineR)
data(decathlon)
pcaoiv <- PCAoiv(decathlon[,1:10], decathlon[,12:13])
plot(pcaoiv, choix = "var", invisible = "quanti.sup")
```

planecontrib Contributions to a plane

## Description

For a given plane of a MCA, computes contributions and squared cosines of the active variables and categories and of the active individuals.

## Usage

planecontrib(resmca, axes $=c(1,2))$

## Arguments

```
    resmca object of class MCA, speMCA or csMCA
    axes numeric vector of length 2, specifying the axes forming the plane to describe.
        Default is c(1,2).
```


## Value

A list of two lists. The first deals with variables :
ctr vector of contributions of the active categories to the plane
$\cos 2 \quad$ vector of squared cosines of the active categories in the plane
vctr vector of contributions of the active variables to the plane
The second deals with observations :
ctr vector of contributions of the observations to the plane
$\cos 2 \quad$ vector of squared cosines of the observations in the plane

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

dimcontrib, tabcontrib

## Examples

```
data(Music)
junk <- c("FrenchPop.NA","Rap.NA","Jazz.NA","Classical.NA","Rock.NA")
mca <- speMCA(Music[,1:5], excl = junk)
co <- planecontrib(mca)
co$var
```

```
plot.csMCA Plot of class specific MCA
```


## Description

Plots a class specific Multiple Correspondence Analysis (resulting from csMCA function), i.e. the clouds of individuals or categories.

## Usage

\#\# S3 method for class 'csMCA'
plot(x, type = "v", axes = 1:2, points = "all", col = "dodgerblue4", app = 0, ...)

## Arguments

\(\left.\begin{array}{ll}x \& object of class csMCA <br>
character string: 'v' to plot the categories (default), 'i' to plot individuals' points, <br>

'inames' to plot individuals' names\end{array}\right]\)| numeric vector of length 2, specifying the components (axes) to plot (c(1,2) is |
| :--- |
| default) |

col color for the points of the individuals or for the labels of the categories (default is 'dodgerblue4')
app numerical value. If 0 (default), only the labels of the categories are plotted and their size is constant; if 1 , only the labels are plotted and their size is proportional to the weights of the categories; if 2, points (triangles) and labels are plotted, and points size is proportional to the weight of the categories.
$\ldots$ further arguments passed to or from other methods, such as cex, cex.main, ...

## Details

A category is considered to be one of the most contributing to a given axis if its contribution is higher than the average contribution, i.e. 100 divided by the total number of categories.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

```
csMCA, textvarsup, conc.ellipse
```


## Examples

```
# class specific MCA on Music example data set
# ignoring every NA values categories
# and focusing on the subset of women,
data(Music)
female <- Music$Gender=="Women"
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- csMCA(Music[,1:5], subcloud = female, excl = junk)
# cloud of categories
plot(mca)
# cloud of most contributing categories
plot(mca,axes=c(2,3), points = "besthv", col = "darkred", app = 1)
```


## Description

Plots Multiple Factor Analysis data, resulting from multiMCA function.

## Usage

\#\# S3 method for class 'multiMCA'
plot (x, type = "v", axes = c(1, 2), points = "all", threshold = 2.58,
groups = 1:x\$call\$ngroups, col = rainbow(x\$call\$ngroups), app = 0, ...)

## Arguments

x
type character string: 'v' to plot the categories (default), 'i' to plot individuals' points, 'inames' to plot individuals' names
axes numeric vector of length 2 , specifying the components (axes) to plot ( $\mathrm{c}(1,2$ ) is default)
points character string. If 'all' all points are plotted (default); if 'besth' only those who are the most correlated to horizontal axis are plotted; if 'bestv' only those who are the most correlated to vertical axis are plotted; if 'best' only those who are the most coorelated to horizontal or vertical axis are plotted.
threshold numeric value. V-test minimal value for the selection of plotted categories.
groups numeric vector specifying the groups of categories to plot. By default, every groups of categories will be plotted
col a color for the points of the individuals or a vector of colors for the labels of the groups of categories (by default, rainbow palette is used)
app numerical value. If 0 (default), only the labels of the categories are plotted and their size is constant; if 1 , only the labels are plotted and their size is proportional to the weights of the categories; if 2, points (triangles) and labels are plotted, and points size is proportional to the weight of the categories.
... further arguments passed to or from other methods, such as cex, cex.main, ...

## Details

A category is considered to be one of the most correlated to a given axis if its test-value is higher then 2.58 (which corresponds to a 0.05 threshold).

## Author(s)

Nicolas Robette

## References

Escofier, B. and Pages, J. (1994) "Multiple Factor Analysis (AFMULT package)". Computational Statistics and Data Analysis, 18, 121-140.

## See Also

multiMCA, textvarsup, speMCA, csMCA

## Examples

```
# specific MCA on music variables of Taste example data set
## another one on movie variables of 'Taste' example data set,
## and then a Multiple Factor Analysis and plots the results.
data(Taste)
# specific MCA on music variables of Taste example data set
mca1 <- speMCA(Taste[,1:5], excl = c(3,6,9,12,15))
# specific MCA on movie variables of Taste example data set
mca2 <- speMCA(Taste[,6:11], excl = c(3,6,9,12,15,18))
# Multiple Factor Analysis
mfa <- multiMCA(list(mca1,mca2))
# plot
plot.multiMCA(mfa, col = c("darkred", "darkblue"))
# plot of the second set of variables (movie)
plot.multiMCA(mfa, groups = 2, app = 1)
```

plot.speMCA Plot of specific MCA

## Description

Plots a specific Multiple Correspondence Analysis (resulting from speMCA function), i.e. the clouds of individuals or categories.

## Usage

\#\# S3 method for class 'speMCA'
plot $(x$, type $=" v "$, axes $=c(1,2)$, points = "all", col = "dodgerblue4", app = 0, $\ldots$ )

## Arguments

x
type
axes numeric vector of length 2, specifying the components (axes) to plot $(\mathrm{c}(1,2)$ is default)
points character string. If 'all' all points are plotted (default); if 'besth' only those who contribute most to horizontal axis are plotted; if 'bestv' only those who contribute most to vertical axis are plotted; if 'besthv' only those who contribute most to horizontal or vertical axis are plotted; if 'best' only those who contribute most to the plane are plotted.
col color for the points of the individuals or for the labels of the categories (default is 'dodgerblue4')
app numerical value. If 0 (default), only the labels of the categories are plotted and their size is constant; if 1 , only the labels are plotted and their size is proportional to the weights of the categories; if 2, points (triangles) and labels are plotted, and points size is proportional to the weight of the categories.
.. further arguments passed to or from other methods, such as cex, cex.main, ...

## Details

A category is considered to be one of the most contributing to a given axis if its contribution is higher than the average contribution, i.e. 100 divided by the total number of categories.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

```
speMCA, textvarsup, conc.ellipse
```


## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# cloud of categories
plot(mca)
```

plot.stMCA
Plot of standardized MCA

## Description

Plots a standardized Multiple Correspondence Analysis (resulting from stMCA function), i.e. the clouds of individuals or categories.

## Usage

```
## S3 method for class 'stMCA'
plot(x, type = "v", axes = 1:2, points = "all", threshold = 2.58, groups=NULL,
    col = "dodgerblue4", app = 0, ...)
```


## Arguments

\(\left.\begin{array}{ll}x \& object of class stMCA <br>
character string: 'v' to plot the categories (default), 'i' to plot individuals' points, <br>

'inames' to plot individuals' names\end{array}\right]\)| numeric vector of length 2, specifying the components (axes) to plot (c(1,2) is |
| :--- |
| default) |
| character string. If 'all' all points are plotted (default); if 'besth' only those who |
| are the most correlated to horizontal axis are plotted; if 'bestv' only those who |
| are the most correlated to vertical axis are plotted; if 'best' only those who are |
| the most coorelated to horizontal or vertical axis are plotted. |

## Details

A category is considered to be one of the most correlated to a given axis if its test-value is higher then 2.58 (which corresponds to a 0.05 threshold).

## Author(s)

Nicolas Robette

## References

Bry X., Robette N., Roueff O., 2016, « A dialogue of the deaf in the statistical theater? Adressing structural effects within a geometric data analysis framework », Quality \& Quantity, 50(3), pp 1009-1020 [https://link.springer.com/article/10.1007/s11135-015-0187-z]

## See Also

stMCA, textvarsup, conc.ellipse

## Examples

```
# standardized MCA of Music example data set
# controlling for age
## and then draws the cloud of categories.
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
stmca <- stMCA(mca, control = list(Music$Age))
# cloud of categories
plot(stmca)
# cloud of categories on dimensions 2 and 3
plot(stmca, axes = c(2,3), points = "best", col = "darkred", app = 1)
```

```
quadrant Quadrant of active individuals
```


## Description

Computes the quadrant of active individuals from a MCA.

## Usage

quadrant (resmca, dim $=c(1,2)$ )

## Arguments

| resmca | object of class MCA, speMCA, or csMCA |
| :--- | :--- |
| $\operatorname{dim}$ | dimensions of the space (default is $c(1,2)$ ) |

## Value

Returns a factor with four levels : upper_left, lower_left, upper_right, lower_right

## Author(s)

Nicolas Robette

## See Also

speMCA, csMCA

## Examples

\# specific MCA of Music example data set data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
\# distribution of the quadrants
table(quadrant(mca, c(1,2)))

## quasindep Quasi-correspondence analysis

## Description

Transforms a symmetrical contingency table so that it can be used for quasi-correspondence analysis, also called correspondence analysis of incomplete contingency table.

## Usage

quasindep(tab, order $=3$, tol $=1 \mathrm{e}-6$ )

## Arguments

tab
order numeric value. Order of reconstitution of the quasi-independence data. Default is 3 .
tol numeric value. The tolerance threshold to be considered for convergence to null during iteration process. Default is 1e-6.

## Details

In order to carry out a "quasi-correspondence analysis", also called "correspondence analysis of incomplete table", the principle is to stop analyzing the differences between the observed data and the situation of independence between the variable in rows and the variable in columns, as it is the case in the classical correspondence analysis, and to consider the differences between the data and a situation of quasi-independence, i.e. independence for some cells of the table only. In the most common situation, it is therefore a matter of applying the independence hypothesis to the offdiagonal cells only and replacing the diagonal with values that do not influence the analysis. Such values are obtained in an iterative way by replacing the numbers of the cells of the diagonal by their third order reconstruction, then by recalculating the correspondence analysis until convergence is reached. The algorithm used is developed in van der Heijden (1992: 11-12).

## Value

An object of the same class and dimensions as tab: the quasi-independence data to be analyzed with Correspondence Analysis.

## Note

This function is adapted from Milan Bouchet-Valat's script in the supplementary material of his article indicated in the reference section.

## References

De Leeuw J et van der Heijden PGM (1985) Quasi-Correspondence Analysis. Leiden: University of Leiden.
Van der Heijden PGM (1992) Three Approaches to Study the Departure from Quasi-independence. Statistica Applicata 4: 465-80.

Bouchet-Valat M (2015) L'analyse statistique des tables de contingence carrées - L'homogamie socioprofessionnelle en France - I, L’analyse des correspondances Bulletin de Méthodologie Sociologique 125: 65-88. [doi:10.1177/0759106314555655](doi:10.1177/0759106314555655)

## Examples

```
## Not run:
tab <- matrix(c(165,49,70,100,48,223,
    6,201,226,212,90,216,
    4,96,446,214,72,77,
    5,84,305,317,126,188,
    3,52,151,190,110,189,
    17,234,310,601,309,1222),
    nrow = 6, ncol = 6, byrow = TRUE)
newtab <- quasindep(tab)
## End(Not run)
```

    rvcoef RV coefficient
    
## Description

Computes the RV coefficient between two groups of numerical variables.

## Usage

$\operatorname{rvcoef}(X a, X b$, row.w $=$ NULL)

## Arguments

Xa data frame with the first group of numerical variables
$\mathrm{Xb} \quad$ data frame with the second group of numerical variables
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.

## Details

$X a$ and $X b$ should have the same number of rows.

## Value

numerical value : the RV coefficient

## Author(s)

Nicolas Robette

## References

Escouffier, Y. (1973) Le traitement des variables vectorielles. Biometrics 29 751-760.

## See Also

coiPCA, coiMCA, multiMCA

## Examples

```
# RV coefficient between decathlon results by sport
# and Rank and Points
library(FactoMineR)
data(decathlon)
Xa <- decathlon[,1:10]
Xb <- decathlon[,11:12]
str(Xa)
str(Xb)
rvcoef(Xa, Xb)
```

speMCA specific MCA

## Description

Performs a specific Multiple Correspondence Analysis, i.e. a variant of MCA that allows to treat undesirable categories as passive categories.

## Usage

speMCA(data, excl $=$ NULL, $n c p=5$, row.w $=$ NULL)

## Arguments

| data | data frame with n rows (individuals) and p columns (categorical variables) |
| :--- | :--- |
| excl | numeric vector indicating the indexes of the "junk" categories (default is NULL). <br> See getindexcat or use i junk interactive function to identify these indexes. It <br> may also be a character vector of junk categories, specified in the form "namevari- <br> able.namecategory" (for instance "gender.male"). |
| ncp | number of dimensions kept in the results (default is 5) |
| row.w | an optional numeric vector of row weights. If NULL (default), a vector of 1 for <br> uniform row weights) |

## Details

Undesirable (i.e. "junk") categories may be of several kinds: infrequent categories (say, <5 percents), heterogeneous categories (e.g. "others") or uninterpretable categories (e.g. "not available"). In these cases, specific MCA may be useful to ignore these categories for the determination of distances between individuals (see references).

If there are NAs in data, these NAs will be automatically considered as junk categories. If one desires more flexibility, data should be recoded to add explicit factor levels for NAs and then excl option may be used to select the junk categories.

## Value

Returns an object of class speMCA, i.e. a list including:
eig a list of vectors containing all the eigenvalues, the percentage of variance, the cumulative percentage of variance, the modified rates and the cumulative modified rates
call a list with informations about input data
ind a list of matrices containing the results for the individuals (coordinates, contributions, squared cosines and total distances)
var a list of matrices containing all the results for the categories and variables (weights, coordinates, squared cosines, categories contributions to axes and cloud, test values (v.test), squared correlation ratio (eta2), variable contributions to axes and cloud, total distances

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

See Also<br>getindexcat, ijunk, plot.speMCA, ggcloud_indiv, ggcloud_variables, csMCA

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# This is equivalent to :
mca <- speMCA(Music[,1:5], excl = c(3,6,9,12,15))
```


## stMCA Standardized MCA

## Description

Performs a standardized Multiple Correspondence Analysis, i.e it takes MCA results and forces all the dimensions to be orthogonal to a supplementary "control" variable.

## Usage

stMCA(resmca, control)

## Arguments

resmca an object of class MCA, speMCA, csMCA or multiMCA
control a list of control variables

## Details

Standardized MCA unfolds in several steps. 1. First, for each dimension of an input MCA, individual coordinates are used as dependent variable in a linear regression model and the 'control' variable is included as covariate in the same model. 2. The residuals from every models are retained and bound together. The resulting data frame is composed of continuous variables and its number of columns is equal to the number of dimensions in the input MCA. 3. Lastly, this data frame is used as input in a Principal Component Analysis.
It is exactly equivalent to MCA with one orthogonal instrumental variable (see MCAoiv)

## Value

Returns an object of class stMCA. This object will be similar to resmca argument, still it does not comprehend modified rates, categories contributions and variables contributions.

## Author(s)

Nicolas Robette

## References

Bry X., Robette N., Roueff O., 2016, « A dialogue of the deaf in the statistical theater? Adressing structural effects within a geometric data analysis framework », Quality \& Quantity, 50(3), pp 1009-1020 [https://link.springer.com/article/10.1007/s11135-015-0187-z]

## See Also

```
plot.stMCA
```


## Examples

```
# standardized MCA of Music example data set
# controlling for age
## and then draws the cloud of categories.
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
stmca <- stMCA(mca, control = list(Music$Age))
```

supind
Statistics for supplementary individuals

## Description

From MCA results, computes statistics (coordinates, squared cosines) for supplementary individuals.

## Usage

supind(resmca, supdata)
indsup(resmca, supdata)

## Arguments

resmca object of class MCA, speMCA or csMCA
supdata data frame with the supplementary individuals. It must have the same factors as the data frame used as input for the initial MCA.

## Value

Returns a list with the following items :

```
coord matrix of individuals coordinates
    cos2 matrix of individuals squared cosines
```


## Note

indsup is softly deprecated. Please use supind instead.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

ggadd_supind,textindsup, supvar, supvars

## Examples

```
# specific MCA of Music example data set
# excluding the first two observations
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[3:nrow(Music),1:5], excl = junk)
# computes coordinates and squared cosines
# of the first two (supplementary) observations
supind(mca,Music[1:2,1:5])
```

supvar Statistics for a categorical supplementary variable

## Description

From MCA results, computes statistics (weights, coordinates, contributions, test-values, variances) for a categorical supplementary variable.

## Usage

supvar(resmca, var)
varsup(resmca, var)

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
var the categorical supplementary variable. It does not need to have been used at the MCA step.

Value
Returns a list:

| weight | numeric vector of categories weights |
| :--- | :--- |
| coord | data frame of categories coordinates |
| cos2 | data frame of categories squared cosines |
| var | data frame of categories within variances, variance between and within cate- <br> gories and variable squared correlation ratio (eta2) |
| typic | data frame of categories typicality test statistics |
| pval | data frame of categories p-values from typicality test statistics |
| cor | data frame of categories correlation coefficients |

## Note

varsup is softly deprecated. Please use supvar instead.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).

Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

supvars, ggadd_supvar, ggadd_supvars, textvarsup, supind

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# computes statistics for Age supplementary variable
supvar(mca,Music$Age)
```


## Description

From MCA results, computes statistics (weights, coordinates, squared cosines, contributions, testvalues, variances) for categorical supplementary variables.

## Usage

supvars(resmca, vars)
varsups(resmca, vars)

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multimCA
vars A data frame of categorical supplementary variables. All these variables should be factors.

## Value

Returns a list with the following items :

| weight | numeric vector of categories weights |
| :--- | :--- |
| coord | data frame of categories coordinates |
| cos2 | data frame of categories squared cosines |
| var | a list of data frames of categories within variances, variance between and within <br> categories and variable square correlation ratio (eta2) |
| typic | data frame of categories typicality test statistics |
| pval | data frame of categories p-values from typicality test statistics |
| cor | data frame of categories correlation coefficients |

Note
varsups is softly deprecated. Please use supvars instead.

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

supvar, ggadd_supvar, ggadd_supvars, textvarsup, supind

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# computes statistics for Gender and Age supplementary variables
supvars(mca, Music[, c("Gender","Age")])
```

tabcontrib

Table with the main contributions of categories to an axis

## Description

Identifies the categories that contribute the most to a given dimension of a Multiple Correspondence Analysis and organizes these informations into a fancy table.

## Usage

tabcontrib(resmca, dim $=1$, best $=$ TRUE, dec $=2$, shortlabs = FALSE)

## Arguments

resmca object of class MCA, speMCA, or csMCA
dim dimension to describe (default is 1st dimension)
best if FALSE, displays all the categories; if TRUE (default), displays only categories with contributions higher than average
dec integer. The number of decimals for the results (default is 2)
shortlabs logical. If TRUE, the data frame will have short column names, so that all columns can be displayed side by side on a laptop screen. Default is FALSE (long explicit column names).

## Value

A data frame with the following contributions.:

| Variable | names of the variables |
| :--- | :--- |
| Category | names of the categories |
| Weight | weights of the categories |

Quality of representation
quality of representation (squared cosine) of the categories on the axis
Contribution (left)
contributions of the categories located on one side of the axis

Contribution (right)
contributions of the categories located on the other side of the axis
Total contribution
contributions summed by variable
Cumulated contribution cumulated sum of the contributions
Contribution of deviation
for each variable, contribution of the deviation between the barycenter of the categories located on one side of the axis and the barycenter of those located on the other side
Proportion to variable
contribution of deviation expressed as a proportion of the contribution of the variable

## Author(s)

Nicolas Robette

## References

Le Roux B. and Rouanet H., Multiple Correspondence Analysis, SAGE, Series: Quantitative Applications in the Social Sciences, Volume 163, CA:Thousand Oaks (2010).
Le Roux B. and Rouanet H., Geometric Data Analysis: From Correspondence Analysis to Stuctured Data Analysis, Kluwer Academic Publishers, Dordrecht (June 2004).

## See Also

dimcontrib, dimdescr, dimeta2, dimtypicality

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# main contributions on axis 1
tabcontrib(mca, 1)
# main contributions on axis 2
tabcontrib(mca, 2)
```

Taste Taste (data)

## Description

The data concerns tastes for music and movies of a set of 2000 individuals. It contains 5 variables of likes for music genres (french pop, rap, rock, jazz and classical), 6 variables of likes for movie genres (comedy, crime, animation, science fiction, love, musical) and 2 additional variables (gender and age).

## Usage

data(Taste)

## Format

A data frame with 2000 observations and the following 13 variables:
FrenchPop factor with levels No , Yes, NA
Rap factor with levels No, Yes, NA
Rock factor with levels No, Yes, NA
Jazz factor with levels No, Yes, NA
Classical factor with levels No, Yes, NA
Comedy factor with levels No, Yes, NA
Crime factor with levels No, Yes, NA
Animation factor with levels No, Yes, NA
SciFi factor with levels No, Yes, NA
Love factor with levels No, Yes, NA
Musical factor with levels No, Yes, NA
Gender factor with levels Men, Women
Age factor with levels 15-24, 25-49, 50+
Educ factor with levels none, low, medium, high

## Details

NA stands for "not available"

## Examples

```
data(Taste)
str(Taste)
```

textindsup Plot of supplementary individuals

## Description

Adds supplementary individuals to a MCA cloud of the individuals.

## Usage

textindsup(resmca, supdata, axes = c(1, 2), col = "darkred")

## Arguments

| resmca | object of class MCA, speMCA, or csMCA |
| :--- | :--- |
| supdata | data frame with the supplementary individuals. It must have the same factors as <br> the data frame used as input for the initial MCA. |
| axes | numeric vector of length 2, specifying the dimensions (axes) to plot (default is <br> $\mathrm{c}(1,2)$ ) |
| col | color for the labels of the categories (default is "darkred") |

## Author(s)

Nicolas Robette

## See Also

supind, plot.speMCA, plot.csMCA

## Examples

```
# specific MCA of Music example data set
# excluding the first two observations
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[3:nrow(Music), 1:5], excl = junk)
# cloud of active individuals
# with the two supplementary individuals
plot(mca, type = "i")
textindsup(mca, Music[1:2, 1:5])
```

```
textvarsup Plot of a categorical supplementary variable
```


## Description

Adds a categorical supplementary variable to a MCA cloud of categories.

## Usage

textvarsup(resmca, var, sel = 1:nlevels(var), axes = c(1, 2), col = "black", app = 0, vname = NULL)

## Arguments

resmca object of class MCA, speMCA, csMCA, stMCA or multiMCA
var the categorical supplementary variable. It does not need to have been used at the MCA step.
sel numeric vector of indexes of the categories of the supplementary variable to be added to the plot (by default, labels are plotted for every categories)

| axes | numeric vector of length 2, specifying the dimensions (axes) to plot (default is <br> $\mathrm{c}(1,2)$ ) |
| :--- | :--- |
| col | color for the labels of the categories (default is black) |
| app | numerical value. If 0 (default), only the labels are plotted and their size is con- <br> stant; if 1, only the labels are plotted and their size is proportional to the weights <br> of the categories; if 2, points (triangles) and labels are plotted, and points size is <br> proportional to the weight of the categories. <br> a character string to be used as a prefix for the labels of the categories (null by <br> default) |

## Author(s)

Nicolas Robette

## See Also

supvar, supvars, plot.speMCA, plot.csMCA

## Examples

```
# specific MCA of Music example data set
data(Music)
junk <- c("FrenchPop.NA", "Rap.NA", "Rock.NA", "Jazz.NA", "Classical.NA")
mca <- speMCA(Music[,1:5], excl = junk)
# cloud of categories
# with Gender and Age supplementary variables
plot(mca, col = "gray")
textvarsup(mca, Music$Gender,col = "darkred")
textvarsup(mca, Music$Age, sel = c(1,3), col = "orange",
    vname = "age", app = 1)
```

translate.logit Deprecated function

## Description

This function has been moved to the translate. logit package.

## Usage

translate.logit(...)

## Arguments

$\ldots \quad$ arguments are ignored

## wCMCA Within-class MCA

## Description

Within-class MCA, also called conditional MCA

## Usage

```
    wCMCA(data, class, excl = NULL, row.w = NULL, ncp = 5)
```


## Arguments

data data frame with only categorical variables, i.e. factors
class factor specifying the class
excl numeric vector indicating the indexes of the "junk" categories (default is NULL). See getindexcat or use ijunk interactive function to identify these indexes. It may also be a character vector of junk categories, specified in the form "namevariable.namecategory" (for instance "gender.male").
row.w numeric vector of row weights. If NULL (default), a vector of 1 for uniform row weights is used.
ncp number of dimensions kept in the results (by default 5)

## Details

Within-class Multiple Correspondence Analysis is a MCA where the active categories are centered on the mean of their class (i.e. conditional frequencies) instead of the overall mean (i.e. marginal frequencies).
It is also known as "conditional MCA" and can be seen as a special case of MCA on orthogonal instrumental variables, with only one (categorical) instrumental variable.

## Value

An object of class speMCA, with an additional item :
ratio the within-class inertia percentage

## Note

The code is adapted from speMCA function.
As in speMCA, if there are NAs in data, these NAs will be automatically considered as junk categories. If one desires more flexibility, data should be recoded to add explicit factor levels for NAs and then excl option may be used to select the junk categories.

## Author(s)

Nicolas Robette

## References

Escofier B., 1990, Analyse des correspondances multiples conditionnelle, La revue de Modulad, 5, 13-28.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

MCAoiv, wcPCA, PCAoiv

## Examples

```
# within-class analysis of tea data
# with SPC as class
library(FactoMineR)
data(tea)
res <- wcMCA(tea[,1:18], tea$SPC)
res$ratio
ggcloud_variables(res)
```

```
wcPCA Within-class Principal Component Analysis
```


## Description

Within-class Principal Component Analysis

## Usage

> wcPCA $(X$, class, scale. unit $=$ TRUE, ncp $=5$, ind. sup $=$ NULL, quanti. sup $=$ NULL, quali.sup $=N U L L$, row.w $=$ NULL, col.w $=$ NULL, graph $=$ FALSE, axes $=c(1,2))$

## Arguments

$\mathrm{X} \quad$ a data frame with $n$ rows (individuals) and $p$ columns (numeric variables)
class factor specifying the class
scale.unit a boolean, if TRUE (default) then data are scaled to unit variance
ncp number of dimensions kept in the results (by default 5)
ind.sup a vector indicating the indexes of the supplementary individuals
quanti.sup a vector indicating the indexes of the quantitative supplementary variables
quali.sup a vector indicating the indexes of the categorical supplementary variables

| row.w | an optional row weights (by default, a vector of 1 for uniform row weights); the <br> weights are given only for the active individuals <br> an optional column weights (by default, uniform column weights); the weights <br> are given only for the active variables |
| :--- | :--- |
| col.w | boolean, if TRUE a graph is displayed. Default is FALSE. |
| graph | a length 2 vector specifying the components to plot |

## Details

Within-class Principal Component Analysis is a PCA where the active variables are centered on the mean of their class instead of the overall mean.
It is a "conditional" PCA and can be seen as a special case of PCA with orthogonal instrumental variables, with only one (categorical) instrumental variable.

## Value

An object of class PCA from FactoMineR package, with an additional item :
ratio the within-class inertia percentage

Note
The code is adapted from PCA function from FactoMineR package.

## Author(s)

Nicolas Robette

## References

Escofier B., 1990, Analyse des correspondances multiples conditionnelle, La revue de Modulad, 5, 13-28.
Lebart L., Morineau A. et Warwick K., 1984, Multivariate Descriptive Statistical Analysis, John Wiley and sons, New-York.)

## See Also

PCAoiv, wcMCA, MCAoiv

## Examples

```
# within-class analysis of decathlon data
# with quatiles of points as class
library(FactoMineR)
data(decathlon)
points <- cut(decathlon$Points, c(7300, 7800, 8000, 8120, 8900), c("Q1", "Q2", "Q3", "Q4"))
res <- wcPCA(decathlon[,1:10], points)
plot(res, choix = "var")
```

wtable Deprecated functions

## Description

These functions have been moved to the descriptio package. You may check its documentation here : https://nicolas-robette.github.io/descriptio/

## Usage

wtable(...)
pem(...)
phi.table(...)
assoc.twocont(...)
assoc.twocat(...)
assoc.catcont(...)
assoc.yx (...)
darma(...)
catdesc(...)
condesc(...)
ggassoc_phiplot(...)
ggassoc_boxplot(...)
ggassoc_scatter(...)
ggassoc_crosstab(...)

## Arguments

$\ldots \quad$ arguments are ignored

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